

MINI-SENTINEL METHODS

STATISTICAL METHODS FOR IMPROVING CONFOUNDER ADJUSTMENT FOR EMERGENT TREATMENT COMPARISON

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I. INTRODUCTION

A. BACKGROUND

Appropriate confounder adjustment is critical in postmarket surveillance because patients are not randomized as in clinical trials. Monitoring newly marketed treatments is particularly challenging due to 1) low uptake of new treatments in the early years of treatment availability; 2) rare occurrence of adverse events (related to low treatment uptake or to the rare nature of the adverse event); and 3) patients treated early during follow-up being different from those treated later (e.g., critically ill patients who do not respond to the standard treatment may be selectively prescribed the new treatment when it is first marketed). Propensity Score (PS) techniques may not be optimal when low use predominates and may require modification as usage increases. Even though Disease Risk Score (DRS) techniques may be advantageous in such scenarios, these too may pose problems when adverse outcomes are rare and/or when potential confounders are strongly associated with treatment.

For this project, we evaluate different statistical choices for confounder adjustment, namely PS and DRS methods and regression, to develop heuristics for confounder adjustment for emerging therapies, and consider expert opinion, feasibility, and results from simulations and literature review to guide our decisions. We then use Mini-Sentinel (M-S) data resources to evaluate implementation of these confounder adjustment methods in a sequential testing framework and provide recommendations for improving confounding adjustment for emergent treatment comparison.

B. SPECIFIC AIMS

This project aims to explore how and whether PS and DRS methods and regression could be implemented to adequately adjust for multiple confounders when evaluating adverse events associated with newly marketed treatments in a sequential testing framework.

II. SIMULATIONS

A. INTRODUCTION/OVERVIEW

We performed simulations to identify optimal confounder adjustment methods under various scenarios in which the frequency of treatment and outcome ranged from rare to common. We then used these results to inform selection of appropriate analytic methods for a methodological example. Incident users in each year of follow-up were used in this simulation study. Disease characteristics and demographic characteristics were measured at entry and were included in propensity score models and disease risk score models. Individuals were not followed longitudinally. For cumulative data runs, individuals from earlier years retain their original covariate values. Their data is used to support models of subsequent years but only new, incident users of each study year are given scores based on these new models.

B. METHODS

1. Simulation of Treatment

We simulated whether an individual receives the treatment of interest (Z=1) or comparator treatment (Z=0) using a logistic regression model (1). We included age (centered at 50 years) in the model as a



continuous variable (x_1) , gender (x_2) , presence of acute disease (x_3) , presence of chronic disease (x_4) , and six other covariates $(x_5,..., x_{10})$ as binary variables. Exact distributions of variables are specified in Section B.8. We defined follow-up time (*t* for year) as discrete times 1 to 10. For each year, there was a new cohort of patients. The follow-up time (*t*) was included in the model (1) as a continuous variable.

Logit $(Z = 1 | x_1, x_2, x_3 ...) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \dots + \beta_{10} x_{10} + \beta_{11} t + \beta_{12} x_4 t$ (1)

In the above model, β_0 is the intercept, β_1 , β_2 , ..., β_{10} are coefficients for confounders x_1 , ..., x_{10} , and β_{11} is the coefficient for time t. Inclusion of the term $\beta_{11}t$ allows the uptake of a new treatment to increase over time steadily. We will also simulate the situation where sicker or healthier individuals may tend to receive the treatment of interest earlier by including the interactions between chronic disease (x_4) and time (t).

2. Simulation of Outcome

At each of the 10 discrete times (t), we simulated the outcome (Y=0 or 1) using model (2).

Logit
$$(Y = 1 | Z, x_1, x_2, x_3 ...) = \theta_0 + \theta_Z Z + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3 + \dots + \theta_{10} x_{10}$$
 (2)

In the above outcome model, θ_0 is the intercept, and $\theta_1, \dots, \theta_{10}$ are the coefficients for confounders x_1, \dots, x_{10} . The parameter for the treatment (θ_Z) represents the log odds ratio of having the outcome for those taking the drug of interest compared to those on the active comparator drug after adjusting for all variables in the model. When the probability of occurrence of adverse events is less than 5%, the odds ratio exp(θ_Z) is approximately the relative risk.

3. PS and DRS Models

The idea of active surveillance is to repeatedly over time assess for the existence of elevated risk of a given outcome due to treatment of interest. For example we may plan to look at the data quarterly and if we do not find evidence for an elevated risk at a given quarter we continue monitoring (e.g., for up to 3 years), but if we do find elevated risk we may signal or alert to conduct a more thorough investigation of the data. To do this in a sequential framework we must incorporate differential confounding over time and handle the sequential testing in which at earlier looks we have estimated a risk that did not indicate a signal and decided to continue monitoring. To properly handle such data we form a sequential monitoring framework that will be discussed in more detail in Section 7. One specific aspect of such a sequential monitoring framework is determining which data should be used at a given analysis or look time. This becomes a larger issue when one is using exposure matching or stratification. Statistically to incorporate a sequential monitoring boundary the exposure matching and stratification categories at previous looks must remain the same (i.e. attempting to keep the population used in previous looks static). However, there are choices in which data to use to fit the current look's DRS and PS models to determine new disease/exposure matches or disease/exposure stratification categories. For this simulation study we have explored two approaches: lookwise estimation and cumulative estimation.

a. Lookwise Estimation

Lookwise estimation uses the current look's incident users to build PS and DRS models.¹ Specifically, let N_t and n_t represent the look specific population size (treatment of interest and comparator treatment) and treatment of interest population size (i.e. number of individuals who received the treatment of



interest (Z=1)) in interval t, respectively. In lookwise estimation, for look t, a propensity score model was fit and each individual's PS(t) was estimated using only the current look's population, N_t and n_t . Then matching and stratification were performed using the look specific PS from look t. An individual remained in his or her stratum in current and subsequent analyses of future looks.

b. Cumulative Estimation

Cumulative estimation uses the cumulative population to the current look (from beginning of surveillance) in building PS and DRS models. Let $\dot{N}(k) = \sum_{t=1}^{k} N_t$ and $\dot{n}(k) = \sum_{t=1}^{k} n_t$ represent the cumulative total and treatment of interest population sizes up to *k*th look, respectively. $PS^c(k)$ denotes the cumulative PS estimated with population sizes $\dot{N}(k)$ and $\dot{n}(k)$. In matching, comparators who were matched to the treatment of interest in previous intervals 1,2,...,(t-1) remained in their previous matched strata. Similarly for stratification those were classified as being within stratum *s* in previous looks remained in stratum *s* for all future looks. Thus, only the incident users in a current look were either matched or reclassified into strata.

Both lookwise and cumulative estimation methods used similar PS and DRS models for computing PSs and DRSs. The PS for an individual is the probability of receiving the treatment of interest given his/her covariate values. For incident users of the treatment of interest and comparators in each look, we fit a logistic regression model with the treatment status as the dependent variable and variables $x_1, ..., x_{10}$ as predictors (propensity score models). After all parameter coefficients were estimated in the propensity score model, PSs were calculated for each individual as

$$PS = \frac{\exp(\hat{\beta}_0 + \hat{\beta}_1 x_1 + \hat{\beta}_2 x_2 + \hat{\beta}_3 x_3 + \dots + \hat{\beta}_{10} x_{10})}{1 + \exp(\hat{\beta}_0 + \hat{\beta}_1 x_1 + \hat{\beta}_2 x_2 + \hat{\beta}_3 x_3 + \dots + \hat{\beta}_{10} x_{10})}$$

where $\hat{\beta}_0$, $\hat{\beta}_1$, ..., $\hat{\beta}_{10}$ are estimated coefficients of intercept and confounders using standard maximum likelihood estimation.

The DRS for an individual is the probability of experiencing an outcome (adverse event) given his/her covariate values. In creating DRS model, we included all covariates $(x_1, ..., x_{10})$ and the treatment variable in the model. ^{2,3,4} Thus, the DRS model was the same as model (2). Inclusion of the treatment in the DRS model is critical. Otherwise the effect of treatment on the outcome will not be represented in the model and the true association of confounders with the outcome will be distorted. Consequently the DRS will be wrong and the results from outcome model will be invalid. Our preliminary results showed that the treatment effect approached to the null if treatment status was not included in DRS model. After all parameters were estimated, DRS was calculated as

$$DRS = \frac{\exp(\hat{\theta}_0 + \hat{\theta}_1 x_1 + \hat{\theta}_2 x_2 + \hat{\theta}_3 x_3 + \dots + \hat{\theta}_{10} x_{10})}{1 + \exp(\hat{\theta}_0 + \hat{\theta}_1 x_1 + \hat{\theta}_2 x_2 + \hat{\theta}_3 x_3 + \dots + \hat{\theta}_{10} x_{10})}$$

where $\hat{\theta}_0$, $\hat{\theta}_1$,..., $\hat{\theta}_{10}$ were estimated from DRS model. Note that even though treatment was included in the DRS model which was used to calculate the parameters, the term $\hat{\theta}_z Z$ was not included (i.e., Z=0) for the entire cohort, in the calculation of DRSs for individual participants.³



In creating PS or DRS models, we anticipated quasi-data separation would occur when treatment or outcome numbers are low (i.e., 20-50 outcome or treatments of interest). To solve this issue in a simulation setting, we used the backward selection approach with a p-value <0.5 as the inclusion criteria to select covariates. In this instance, it was not feasible to select variables based on a *priori* knowledge, as we were performing 1000 replicate simulations per each combination of simulation parameters.

Once DRS and PS were calculated, we performed score matching or stratification to create analytic datasets for sequential analyses as detailed in the following section.

4. Matching and Stratification

We performed 1:1 and 1:4 matching on closest values of PS or DRS for different treatment and outcome scenarios ranging from rare to common. Participants matched in previous looks were not re-matched in subsequent time intervals. As incident users were used, individuals receiving the treatment of interest who were not matched in previous looks were not re-used in subsequent looks. For most simulations, we limited the matching ratio to 1:4 because little additional statistical power is gained with additional matches. However, for rare treatment and rare outcome scenarios, we also performed 1:8 matching in order to increase the number of individuals and adverse events in sequential analyses.

We also stratified participants based on percentiles of PS or DRS and performed stratified analyses. At each look, PSs and DRSs were computed using either lookwise or cumulative estimation methods, and each subject was assigned to a stratum based on his/her scores; the subject remained in the stratum throughout following sequential analyses. We explored the impact of different number of strata on parameter estimates and found no significant difference among 5, 10, and 20 strata (Appendix Tables A2 – A3). Thus, we used 10 strata for all simulations.

5. Evaluating Treatment-Outcome Associations after Matching or Stratification

We used conditional logistic regression to evaluate treatment-outcome associations for all analyses matched on PSs or DRSs.

For stratified analyses, we explored different regression methods including Mantel-Haenszel logistic regression⁵, which required pooling results from individual stratum, Firth method which corrects bias when outcome is rare in logistic regression⁶, and fixed effects and random effects logistic regression in which stratum indicators were treated as fixed effects and random effects⁷, respectively (Tables A2-A3). We obtained comparable estimates of treatment effects for conditional, fixed effects, and random effects regression and we opted to perform all stratified analyses using conditional logistic regression, as this method is commonly used in the existing literature. In addition, by using the same outcome model for matching and stratification, we could better ensure that any difference observed in the results could be attributed to different methodological approaches rather than analytic models.

6. Evaluating Treatment-Outcome Associations Using Regression

The regression model for evaluating the association between treatment and outcome was the same as model (2). When we experienced a model convergence problem for rare (~20 events) and moderately rare event (~50 events) scenarios we resorted to using a backward selection procedure with p<0.5 as the significance level for inclusion of covariates, as it was not possible to individually select appropriate confounders for each of the 1000 replicate simulations.



7. Methods for Longitudinal Sequential Estimation

To incorporate group sequential monitoring to form boundaries we used Lan-Demets Group Sequential approach.⁸ This method uses an error spending approach and derives asymptotically normal sequential boundaries taking into account sequential testing of the data following a specified error spending function. Note that in Mini-Sentinel most boundaries applied have used exact methods to form sequential boundaries, but since the emphasis of this workgroup was to compare PS versus DRS we simplified the boundary formation to allow for more extensive simulations to be conducted towards the goals of the workgroup. We maintained an overall one-sided significance level of 0.05 in the sequential analyses. For this simulation we chose to use the Pocock error spending function, $\alpha(t) = \log \left[1 + \frac{1}{2}\right]$

 $(\exp(t) - 1)\frac{\dot{N}_t}{\dot{N}_T} \alpha$ (where α is the overall type I error), that attempts to spend the error so that on the standardized test statistic scale the boundary is approximately flat.²¹ This is the most commonly used shape of the boundary for postmarket surveillance. The test statistic to compare to the sequential

boundary was the standardized Wald test statistic, $\hat{\theta}_z / \sqrt{\operatorname{var}(\hat{\theta}_z)}$ and was calculated at each pre-

specified look time (t=1,...,10). These boundaries are the critical values of the sequential hypothesis tests. After each interim test, if the test statistic is less than the boundary at time t, the trial is continued. When the test statistic is greater than the boundary at time t, the null hypothesis of equal means is rejected and the trial is stopped early.

8. Parameters for Simulating Treatment and Outcome

We simulated 1000 replicate populations, each consisting of 50,000 participants (5,000 per year). We created replicate cohorts by looping back through the code with different starting seed numbers in the randomization routines.

In each population, age was a normally distributed variable with a mean of 50 and a standard deviation of five. This resulted in an age range of 30 – 70 years. The population consisted of 70% of one gender (in this instance, assumed to be male) and 30% of the other (female). We assumed the prevalence of acute disease to be 5% during any given time interval and the prevalence of chronic disease to be 5%. We also included follow-up time and an interaction term between follow-up time and chronic disease to model an increase in chronic disease over time in simulating treatment status. In addition, we included six other covariates with a prevalence of 5%.

We simulated three different scenarios related to strengths of confounding effects. In the first scenario, the strengths of the associations between the confounders $x_1, ..., x_4$ and the treatment and confounders, $x_1, ..., x_4$ and the outcome were the same. In the second scenario, these confounders were more strongly associated with the treatment. In the third, they were more strongly associated with the outcome. Varying the confounding strengths enabled comparison between the PS and DRS methods of confounding adjustment in observational studies. Details of parameter coefficients for these three scenarios are provided in Table 1, for one example simulation (common treatment (~500 in the first year increasing to ~1000 in year 10) and rare outcome (~20 outcomes per year)).



		CON	IFOUNDING STRE	NGTH SCENARIO	S		
	1 (ed	qual)	2 (toward	treatment)	3 (toward	outcome)	
Parameters	Coefficients	Coefficients	Coefficients	Coefficients	Coefficients	Coefficients	
	for the	for the	for the	for the	for the	for the	
	treatment		treatment	outcome	treatment	outcome	
	probabilities	probabilities	probabilities	probabilities	probabilities	probabilities	
Intercept ⁺	-2.5	-6.0	-3.3	-6.0	-2.5	-6.85	
Age	0.002	0.002	0.01	0.002	0.002	0.01	
Gender	0.2	0.2	1.0	0.2	0.2	1.0	
Acute Disease	0.15	0.15	0.75	0.15	0.15	0.75	
Chronic	0.15	0.15	0.75	0.15	0.15	0.75	
Disease							
Time (t)	0.1	0.1	0.1	0.1	0.1	0.1	
Chronic	0.2	NA	0.2	NA	0.2	NA	
Disease*t							
<i>x</i> ₅	0.1	0.1	0.1	0.1	0.1	0.1	
<i>x</i> ₆	0.1	0.1	0.1	0.1	0.1	0.1	
<i>x</i> ₇	0.1	0.1	0.1	0.1	0.1	0.1	
<i>x</i> ₈	0.1	0.1	0.1	0.1	0.1	0.1	
<i>x</i> ₉	0.1	0.1	0.1	0.1	0.1	0.1	
<i>x</i> ₁₀	0.1	0.1	0.1	0.1	0.1	0.1	
treatment	NA	0, 0.69	NA	0, 0.69	NA	0, 0.69	

Table 1. Parameter coefficients for different confounding strength

⁺Intercept parameters in this table are based on the rare outcome (<20/5000) and common treatment (>500/5000) scenario. Intercept coefficients for all scenarios are available in Appendix Table A1.

To make valid comparisons of type I rates and empirical power across different scenarios, we chose different intercepts for different scenarios so that the frequencies of treatments and outcomes were similar. We varied the intercepts in models (1) and (2) to achieve different prevalence of treatment of interest and outcomes ranging from rare, moderately rare, and common (Table 2). The simulated rare treatment and rare outcome may be less applicable to typical Mini-Sentinel projects because the treatment and outcome numbers are very low. A sample of frequencies of treatments and outcomes are listed in Table 3a (rare outcome and common treatment) and Table 3b (common treatment and common outcome).

TREATMENT (\overline{n})	OUTCO	эм
Increasing treatment	A	ver
frequency	0	utc
	,	

Table 2. Simulated treatment and outcome

TRE	ATMENT (<i>n</i>)	OUTCOME (<i>y</i>)				
	Increasing treatment		Average number of			
	frequency		outcomes			
	look 1 to 10		(consistent all looks)			
Rare	25	Rare	<20			
Rare	25	Moderate	50			
Rare	25	Common	200-250			
Moderate	50	Rare	<20			
Moderate	50	Moderate	50			
Moderate	50	Common	200-250			
Common	>500	Rare	<20			



TRE	ATMENT (\overline{n})	OUTCOME (y)				
Common	>500	Moderate	50			
Common	>500	Common	200-250			

Table 3a. Average number of outcomes (\overline{y}) and average number of participants receiving the treatment of interest (\overline{n}) across years in common treatment and rare outcome scenarios (\leq 20 outcomes; OR=1)

	CONFOUNDING STRENGTH SCENARIOS										
	SCENARIO 1		SCENARIO 2		SCENARIO 3						
YEAR	\overline{y}	\overline{n}	\overline{y}	\overline{n}	\overline{y}	\overline{n}					
1	17	514	17	516	16	514					
2	17	549	18	547	16	549					
3	16	614	17	621	16	614					
4	17	662	17	650	17	662					
5	17	727	17	727	17	727					
6	18	759	18	771	17	759					
7	18	849	18	835	17	849					
8	18	916	18	893	17	916					
9	18	997	18	968	17	997					
10	18	1080	18	1057	18	1080					

Table 3b. Average number of outcomes (\overline{y}) and average number of participants receiving the treatment of interest (\overline{n}) across years in common treatment and outcome scenarios (>200 outcomes; OR=1)

	SCENARIO 1		SCENARIO 2		SCENARIO 3		
YEAR	\overline{y}	\overline{y} \overline{n}		\overline{n}	\overline{y}	\overline{n}	
1	218	508	218	513	213	507	
2	218	553	218	556	212	553	
3	217	606	217	606	213	606	
4	218	656	219	656	214	656	
5	217	718	217	714	213	718	
6	219	779	219	773	214	779	
7	219	848	219	838	214	849	
8	218	919	218	906	212	919	
9	217	1000	217	980	214	1000	
10	218	1078	218	1054	214	1078	



9. Evaluation Measures

We evaluated the different confounder adjustment methods according to the following evaluation metrics:

- type I error rates (false positive rates) which were calculated as the percentage of datasets that rejected the null hypothesis $\theta_z = 0$ when data were simulated under $\theta_z = 0$;
- bias which was calculated as the difference between the estimated treatment parameter θ_z and the true treatment parameter under which the data were simulated;
- power to detect an association which was calculated as the percentage of datasets that rejected the null hypothesis $\theta_Z = 0$ when simulations were performed under the true alternative $\theta_Z > 0$; and
- time to signal detection which is from the start of monitoring (i.e., year one in simulation) to the time when the test statistic is greater than the boundary.

C. RESULTS

The results from all simulations performed on a yearly basis are presented in Appendix B. Our main observations in regard to type I error rates, empirical power, treatment effect estimates, and time to signal for the different analysis methods are summarized below.

- 1. In general, we observed no difference between lookwise and cumulative estimation methods.
- In general, we observed no difference between PS and DRS approaches. This result is consistent with a cross-sectional observational study by Arbogast and Ray³, showing that DRS and PS approaches yielded comparable risk estimates when DRS and PS models were correctly specified.
- 3. Empirical power and type I error rates did not differ with different strengths of associations 1) between confounders and treatment, and 2) between confounders and outcome, except in the following scenarios:
 - a) Matching 1:4 or stratifying on PSs or DRSs in rare treatment and rare outcome settings: When treatment and outcome counts were rare, the type I error rates were higher for scenario 1 (equal association strength of confounders with treatment of interest and outcome) when matching 1:4 on PSs or DRSs compared to scenarios 2 (stronger association of confounders with treatment of interest than outcome) and 3 (stronger association of confounders with outcome than treatment of interest) (Table 4). In addition, 1:4 matching on PSs yielded a higher empirical power (14.7%) for scenario 1 compared to scenarios 2 and 3 (5.1% and 5.8%) (Table 5). Similar results were observed in regard to power when matching 1:4 on DRSs;
 - b) Matching 1:4 on PSs and DRSs in the common treatment and common outcome setting. When matching 1:4 on PS, there was a 96% increase in type I error rates between scenarios 1 and 2 (5.6% vs 111%), and a 69% decrease between scenarios 2 and 3 (11% vs 3.4). Similar results were observed when matching 1:4 and stratifying on DRSs.



METHOD	RARE TREATMENT AND RARE OUTCOME			MODERATE TREATMENT AND MODERATE OUTCOME			COMMON TREATMENT AND COMMON OUTCOME			RARE TREATMENT AND MODERATE OUTCOME			MODERATE TREATMENT AND RARE OUTCOME		
	Scenario		l.	Scenario		Scenario			Scenario			Scenario			
	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3
PS 1:1	0.0	0	0	0.7	0.7	0.2	5.8	5.5	2.2	0.0	0	0	0	0	0
PS 1:4	2.0	0.9	1.0	5.8	5.9	4.5	5.6	11.0	3.4	3.8	4.3	3.9	2.8	3.4	3.7
PS	10.4	11	10.	8.6	9.7	8.5	5.5	5.0	2.9	8.7	8.7	10.5	9.0	8.6	9.0
stratification			9												
DRS 1:1	0.0	0	0	0.5	0.8	0.2	6.3	11.4	3.7	0.0	0	0	0	0	0
DRS 1:4	1.6	0.8	0.5	5.2	6.8	4.5	6.3	17.8	5.3	4.6	4.1	3.8	3.1	3.5	3.8
DRS	10.1	10.7	11.	8.8	9.9	8.4	6.8	18.1	4.4	9.0	9.3	10.1	9.2	8.6	8.1
stratification			6												

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Table 5. Empirical power with lookwise estimation method for computing PS and DRS under OR=2 ($\theta_Z = 0.693$)

METHOD	D RARE TREATMENT AND RARE OUTCOME Scenario		M TREA M O	ODERAT TMENT ODERAT UTCOM	re AND re E	CO TREAT CO OL	MMON MENT MMON	N AND N E	RARE AND C	TREATM MODEF OUTCOM	ИЕNT RATE E	M TREA RARI	ODERA TMENT E OUTC	TE AND OME	
)	Scenario			Scenario			Scenario			Scenario		
	1	2	3	1	2	3	1	2	3	1	2	3	1	2	3
PS 1:1	0.0	0.0	0.0	19.7	16.9	15.8	100	100	100	1.0	2.1	1.4	0.7	1.5	0.8
PS 1:4	14.7	5.1	5.8	50.9	49.4	50.0	100	100	100	28.2	28.8	30.3	24.8	30.6	28.1
PS strati- fication	36.4	30.6	30.8	65.7	66.8	65.4	100	100	100	44.8	47.4	48.5	39.7	44.4	46.6
DRS 1:1	0.0	0.0	0.0	17.2	16.1	16.1	100	100	100	1.3	2.0	1.5	0.6	1.5	0.7
DRS 1:4	13.3	4.7	5.7	49.6	50.9	50.9	100	100	100	30.9	30.4	30.8	24.3	29.7	27.3
DRS stra- tification	36.0	30.6	31.0	65.9	67.5	65.2	100	100	100	45.2	49.4	49.1	38.9	44.2	45.1

4. Matching methods using a 1:1 ratio yielded lower empirical power: When both treatment and outcomes were rare or moderately rare, we observed very different results in empirical power for 1:1 matching compared to 1:4 matching (Table 6). The 1:4 matching had clear benefits in empirical power when outcome or treatment counts were relatively low, but the benefits were less apparent when treatments or outcomes were common. The ratio of the empirical power between 1:4 matching versus 1:1 matching decreased when there were more treatments and/or outcomes. For example, when the treatment of interest and outcome were rare, the ratio was infinite (14.7% empirical power for 1:4 matching versus zero empirical power for 1:1); when the outcome became moderate, the ratio was 28.2 (28.2% empirical power for 1:4 matching versus 1% empirical power for 1:4); when the outcome became common, the ratio dropped to 1.72 (72.6% empirical power for 1:4 matching versus 42.0% empirical power for 1:1).



In the rare outcome setting, the ratio was infinite (14.7% empirical power for 1:4 matching versus zero empirical power for 1:1 matching) when treatment was rare; it decreased to 35.4 (24.8% empirical power for 1:4 matching versus 0.7% empirical power for 1:1 matching) when treatment was moderately rare; it further decreased to 1.3 (95.5% empirical power for 1:4 matching versus 76.4% empirical power for 1:1 matching) when treatment was common. When the OR increased to 5, we observed similar trends (Appendix Table A6a, A6b, and A6c). We also explored 1:8 matching on PS using the lookwise estimation method for scenario 1 (equal strengths of associations between confounders and the treatment and confounders and the outcome). This increased empirical power to 22.8%, which is significantly higher than the 14.7% observed for 1:4 matching. However, it remained lower than the 36.4% we observed when stratifying on PS.

METHOD	RARE TREATMENT			MOD	ERATE TREAT	MENT	COMMON TREATMENT			
	Rare Moderate Commo		Common	Rare	Moderate Common		Rare	Moderate	Common	
	outcome	outcome	outcome	outcome	outcome	outcome	outcome	outcome	outcome	
PS 1:1	0.0	1.0	42.0	0.7	19.7	77.4	76.4	99.8	100	
PS 1:4	14.7	28.2	72.6	24.8	50.9	93.4	95.5	100	100	
DRS 1:1	0.0	1.3	44.2	0.6	17.2	78.0	78.8	100	100	
DRS 1:4	13.3	30.9	73.3	24.3	49.6	94.0	95.7	100	100	

Table 6. Empirical power comparing 1:1 and 1:4 matching with lookwise estimation method and scenario 1 of confounding strength under OR=2 ($\theta_Z = 0.693$)

5. Stratification: yielded higher type I error rates and inflated empirical power in all scenarios except when the treatment of interest was common. This is likely caused by overestimated treatment effects as discussed below.

Stratification kept all adverse events BUT resulted in higher than nominal type I error rates (2.0% for PS 1:4 matching versus 10.4% for PS stratification) when treatment and outcome were rare, indicating that using this approach may result in inflated power (Table 7). Table 8 shows the mean treatment effect coefficients and standard deviations for all the approaches by years of follow-up, and for those datasets that had valid treatment effect estimates. A treatment effect estimate between -12 and 12 in SAS output was considered valid. Examination of 1000 treatment effect estimates confirmed the need to exclude extreme values. In general, for the matching approach, the 1:1 matching ratio underestimated treatment effects. For example, in year 1, the mean parameter estimates for records with valid estimates were 0.001 and 0.002 for PS and DRS approaches, respectively. These values were well below the simulated 0.693. These estimates increased over the years, but only reached to a maximum value of 0.402 for PS 1:1 matching approach and 0.432 for DRS 1:1 matching approach at year 10. This pattern explains the lower empirical power of 1:1 matching when treatment and outcomes are rare; Estimates from 1:4 matching had higher initial values (0.08-0.09) which increased from year 1 to year 5 to reach levels exceeding the simulated 0.693 (~0.90) and decreased afterward to levels closer to the true value of the treatment parameter by year 10 (0.69-0.70). At year 1, the valid initial estimates from stratification (N~200) were close to or exceeded the simulated level (PS: 0.89; DRS: 0.65). These estimates then increased from year 1 to year 3 and decreased afterwards to levels slightly below the true value (PS: 0.61; DRS: 0.60). Compared to 1:4 matching,



stratification overestimated treatment effects in the early years (2, 3, 4 and 5). This may explain the inflated empirical power observed when using stratification in the annual sequential analyses.

The inflation of empirical power by stratification was greatest when both treatment and outcome were rare, and lessened with increasing incidence of treatment and/or outcomes (Table 9). For example, in rare treatment and rare outcome settings, the ratio of empirical power between stratification and 1:4 matching on PS was 2.48 (36.4%/14.7%=2.48). This decreased to 1.59 (44.8%/28.2%=1.59) in scenarios in which the outcome was moderately rare, and further decreased to 1.14 (82.7%/72.6%=1.14) in common outcome scenarios. With the increased incidence of treatment, we also observed a decrease in the inflation of empirical power. For example, the ratio of powers between stratification and PS matching1:4 was 2.48 (36.4%/14.7%=2.48) when both treatment and outcome were rare. This ratio decreased to 1.60 in settings with moderately rare treatment, and further decreased to 1.01 in scenarios where treatment was common (96.2%/95.5%=1.01). Similar patterns were observed when matching and stratifying on DRSs, and for scenarios 2 and 3.

		TREATMENT PARAMETER $\theta_Z = 0.693$ (OR=2)						
Design and	$\theta_Z = 0$	Signaled %	MEAN d	$\hat{\theta}_{Z}$ (STD)	Mean Time to	Median Time to		
Method	Type 1		Signaled	Signaled	Signal	Signal Detection		
	Error %			and Not, N	Detection (STD)	(5%, 95%)		
PS Matching	0.0	0.0	NA	0.40 (0.71),	NA	NA		
1:1				712				
PS Matching	2.0	14.7	1.94 (0.48)	0.74 (0.80),	8.19 (1.68)	8 (5 10)		
1:4				929				
PS Stratification	10.4	36.4	1.91 (0.66)	0.93 (0.96),	4.95 (3.15)	5 (1 10)		
				932				
DRS Matching	0.0	0.0	NA	0.44 (0.75),	NA	NA		
1:1				711				
DRS Matching	1.6	13.3	1.94 (0.45)	0.73 (0.78),	8.11 (1.70)	8 (5 10)		
1:4				930				
DRS	10.1	36.0	1.93 (0.66)	0.93 (0.96),	4.84 (3.13)	4 (1 10)		
Stratification				929				
Regression	10	35.9	1.93 (0.67)	1.50 (0.78),	4.81 (3.08)	4 (1 10)		
				572				

Table 7. Rare treatment rare outcome: regression and lookwise estimation method and scenario 1 of confounding strength



YEAR				PS	DRS					
	1::	1 match	1:4	4 match	stra	tification	1	:1 match	1	:4 match
	Ν	Mean $\widehat{\theta}_Z$	Ν	Mean $\widehat{\theta}_Z$	Ν	Mean $\widehat{\theta}_Z$	Ν	Mean $\widehat{\theta}_Z$	Ν	Mean $\hat{\theta}_Z$
		(std)		(std)		(std)		(std)		(std)
1	798	0.001	646	0.085	205	-0.893	776	0.002	622	0.077
		(0.052)		(0.352)		(6.001)		(0.047)		(0.326)
2	643	-0.0002	491	0.426	300	1.767	635	0.001	494	0.388
		(0.103)		(0.664)		(1.111)		(0.101)		(0.637)
3	561	0.020	475	0.725	420	1.449	554	0.005	476	0.707
		(0.208)		(0.711)		(0.378)		(0.191)		(0.723)
4	514	0.054	520	0.878	519	1.199	517	0.029	511	0.867
		(0.332)		(0.714)		(0.436)		(0.314)		(0.737)
5	488	0.101	589	0.932	625	1.017	497	0.089	605	0.887
		(0.446)		(0.719)		(0.480)		(0.445)		(0.741)
6	515	0.146	676	0.902	703	0.882	502	0.165	678	0.898
		(0.523)		(0.719)		(0.505)		(0.538)		(0.744)
7	527	0.209	765	0.880	781	0.781	550	0.242	770	0.862
		(0.597)		(0.757)		(0.526)		(0.616)		(0.750)
8	583	0.266	841	0.782	849	0.676	595	0.311	841	0.779
		(0.667)		(0.751)		(0.553)		(0.681)		(0.769)
9	644	0.372	893	0.747	898	0.640	664	0.375	896	0.741
		(0.696)		(0.760)		(0.558)		(0.711)		(0.744)
10	712	0.402	929	0.703	932	0.605	711	0.432	930	0.685
		(0.712)		(0.748)		(0.559)		(0.745)		(0.720)

Table 8. Number of valid treatment effects (N) and treatment effects (standard deviation) when treatment and outcome were rare for scenario 1 of confounding strength under θ_z =0.693

Table 8 continued

YEAR	DRS		REGRES	SSION
	STRATIFICATION			
	Ν	Mean $\widehat{oldsymbol{ heta}}_Z$ (std)	Ν	Mean $\widehat{ heta}_Z$ (std)
1	200	-0.654 (5.847)	152	2.632 (0.448)
2	300	1.764 (1.112)	298	1.839 (0.371)
3	420	1.448 (0.374)	420	1.442 (0.372)
4	518	1.199 (0.429)	490	1.224 (0.420)
5	622	1.019 (0.478)	401	1.268 (0.405)
6	700	0.883 (0.503)	385	1.274 (0.314)
7	778	0.778 (0.525)	483	1.132 (0.316)
8	846	0.674 (0.554)	558	1.011 (0.335)
9	895	0.637 (0.559)	579	0.972 (0.327)
10	929	0.600 (0.560)	550	0.982 (0.291)

Table 9. Stratification approach inflated empirical power (%) and the problem is lessened with increasing number of treatments and number of outcomes for scenario 1 of confounding strength under θ_z =0.693

METHOD	RARE TREATMENT			MODERATE TREATMENT			COMMON TREATMENT		
	Rare	Moderate	Common	Rare	Moderate	Common	Rare	Moderate	Common
	outcome	outcome	outcome	outcome	outcome	outcome	outcome	outcome	outcome
PS 1:4	14.7	28.2	72.6	24.8	50.9	93.4	95.5	100	100
PS strat-	36.4	44.8	82.7	39.7	65.7	97.6	96.2	100	100
ification									
DRS 1:4	13.3	30.9	73.3	24.3	49.6	94.0	95.7	100	100
DRS stra-	36.0	45.2	83.7	38.9	65.9	97.0	95.8	100	100
tification									
Regress-	35.9	44.9	82.8	39.2	65.1	96.4	96.5	100	100
ion									

- 6. Regression: Similar to stratification, regression yielded higher type I error rates and inflated empirical power in all scenarios except when the treatment of interest was common. This is likely caused by overestimated treatment effects (Table 7-9).
- 7. Comparison of annual and biennial sequential analyses: To examine whether less frequent sequential analyses would increase empirical power, we conducted simulations on a biennial basis, where we created scores and performed sequential analyses every two years. The upper boundaries using Lan-Demets Group Sequential approach for rejecting the null hypothesis are given in Table 10 for both the primary annual analyses and the biennial analyses. Because there were fewer looks during the ten years of follow-up, the upper boundaries for the biennial sequential analyses were lower than those for annual sequential analyses. Biennial sequential analyses increased the empirical power for matching approaches, although not substantially, and the empirical power for stratification remained stable or decreased (Table 11). For example, in scenario 1 (equal confounding strength between confounders and treatment and confounders and the outcome), the empirical power increased from 14.7% to 17.6% when biennial sequential was conducted for 1:4 matching approach whereas the empirical power decreased slightly for the PS stratification approach. Consistent with the power changes, the treatment effects estimates increased for the 1:4 matching approach at years 4 and 6 (Table 12) while the treatment effects estimates did not change for the stratification approach. Similar results were observed for scenarios 2 (stronger associations between confounders and treatment) and 3 (stronger associations between confounders and outcome). The increase in empirical power was less when treatment and outcome were moderately rare (data not shown).

LOOK	ANNUAL	BIENNIAL	LOOK	ANNUAL	BIENNIAL
1	2.412202		6	2.225038	2.113224
2	2.362529	2.176211	7	2.204309	
3	2.316565		8	2.186592	2.089523
4	2.279599	2.143710	9	2.171227	
5	2.249699		10	2.157767	2.070907

Table 10. Boundaries based on Lan-Demets Group Sequential approach



Table 11. Comparison of annual and biennial sequential analyses for rare treatment rare outcome using lookwise estimation method for creating PS or DRS scores for confounding strength scenarios 1, 2 and 3 under θ_z =0.693

		ANNUAL SEQUENTIAL ANALYSES			BIENNIAL SEQUENTIAL ANALYSES			
CONFO- UNDING	Design and Method	Signale d %	Mean $\hat{\theta}_Z$ (std),	Mean Time to Signal	Signale d %	Mean $\hat{\theta}_Z$ (std),	Mean Time to Signal	
IOS			Not. N	(STD)		Not. N	(STD)	
1	PS Matching 1:1	0.0	0.40 (0.71), 712	NA	0.1	0.41 (0.73)	10 (NA)	
	PS Matching 1:4	14.7	0.74 (0.80), 929	8.19 (1.68)	17.6	0.79 (0.87), 931	7.83 (1.92)	
	Stratification	36.4	0.93 (0.96), 932	4.95 (3.15)	32.9	0.80 (0.78), 932	5.98 (2.82)	
	DRS Matching 1:1	0.0	0.44 (0.75), 711	NA	0.1	0.40 (0.71), 724	10 (NA)	
	DRS Matching 1:4	13.3	0.73 (0.78), 930	8.11 (1.70)	16.1	0.78 (0.83), 923	7.90 (2.06)	
	Stratification	36.0	0.93 (0.96), 929	4.84 (3.13)	32.7	0.79 (0.78), 931	5.96 (2.80)	
2	PS Matching 1:1	0.0	0.23 (0.63), 711	NA	0.0	0.25 (0.64), 568	NA	
	PS Matching 1:4	5.1	0.85 (0.77), 799	8.67 (1.70)	7.6	0.83 (0.81), 798	8.26 (2.14)	
	Stratification	30.6	1.14 (1.01), 818	4.86 (3.29)	31.8	1.04 (0.85), 834	5.58 (3.17)	
	DRS Matching 1:1	0.0	0.22 (0.62), 569	NA	0.0	0.28 (0.61), 588	NA	
	DRS Matching 1:4	4.7	0.84 (0.79), 805	8.70 (1.63)	6.8	0.87 (0.77), 814	8.16 (2.07)	
	Stratification	30.6	1.14 (1.02), 818	4.82 (3.32)	30.8	1.02 (0.84), 834	5.64 (3.07)	
3	PS Matching 1:1	0.0	0.19 (0.60), 528	NA	0.0	0.25 (0.56), 504	NA	
	PS Matching 1:4	5.8	0.92 (0.81), 762	8.52 (1.50)	8.8	0.94 (0.81), 758	8.73 (1.56)	
	Stratification	30.8	1.26 (1.06), 784	4.45 (3.19)	34.8	1.11 (1.07), 796	5.02 (3.05)	
	DRS Matching 1:1	0.0	0.22 (0.57), 526	NA	0.0	0.16 (0.57), 490	NA	
	DRS Matching 1:4	5.7	0.92 (0.80), 755	8.42 (1.69)	8.2	0.98 (0.80), 760	8.49 (1.72)	
	Stratification	31.0	1.27 (1.05), 783	4.40 (3.17)	30.0	1.10 (1.07), 776	5.11 (3.05)	

YEAR	1:4 MATCHING ANNUAL		1:4 MATCHING BIANNUAL		STRATIFICATION ANNUAL		STRATIFICATION BIANNUAL	
	N*	Mean $\widehat{oldsymbol{ heta}}_Z$ (std)	N	Mean $\widehat{oldsymbol{ heta}}_Z$ (std)	Ν	Mean $\widehat{ heta}_Z$ (std)	N	Mean $\widehat{ heta}_{Z}$ (std)
2	491	0.426 (0.664)	482	0.411 (0.670)	301	1.722 (1.331)	300	1.767 (1.111)
4	520	0.878 (0.714)	515	0.914 (0.710)	519	1.200 (0.434)	519	1.199 (0.436)
6	676	0.902 (0.719)	678	0.944 (0.745)	703	0.885 (0.501)	703	0.882 (0.505)
8	841	0.782 (0.751)	832	0.803 (0.803)	849	0.679 (0.551)	849	0.676 (0.553)
10	929	0.703 (0.748)	931	0.715 (0.773)	932	0.607 (0.558)	932	0.605 (0.559)

Table 12. Comparison of annual and biennial sequential analyses for rare treatment rare outcome using lookwise estimation method for scenario 1: treatment effect estimate <u>over time</u> under θ_z =0.693

*Number of valid estimates of treatment effect out of 1000 replicates.

III. METHODOLOGICAL EXAMPLE

A. SELECTION CRITERIA

Our criteria for selection of a methodological example included the following: the selected medical product should have known adverse events and have known confounders from prior research; it should have varying use in the population during the given study timeframe, and should be prescribed to participants with varying characteristics over time; the outcomes of interest need to range from rare to more common and should have available data in the MSDD during the study timeframe. As examples from previous or ongoing M-S projects did not meet these criteria, we selected Cyclo-Oxygenase-2 (COX-2) Inhibitors, a class of Non-Steroid Anti-Inflammatory Drugs (NSAIDs), as our exposure of interest and Non-Selective NSAIDs as the active comparator, and evaluated the association between these NSAIDs and gastrointestinal (GI) bleeding events.

B. METHODS

1. NSAID Use and Risk of Adverse Events

NSAIDS are frequently prescribed to alleviate pain due to inflammation caused by ailments such as osteoarthritis. Currently available NSAIDs operate by blocking COX enzymes. These enzymes include COX-1 which protects the lining of the stomach from acid, COX-2, found in joints and muscle, which mediates effects on pain and inflammation, and COX-3, located in the cerebral cortex, which is possibly associated with centrally mediated pain. Non-Selective NSAIDs that block COX-1 and COX-2 reduce pain, but may also cause gastrointestinal bleeding. On the other hand, COX-2 Selective Inhibitor drugs selectively block the COX-2 enzyme and were developed with the expectation that these should be safer with regard to gastrointestinal bleeding. Research studies have generally confirmed lower GI bleeding rates for COX-2 inhibitor use, but some studies have found them to be associated with increased risk of serious cardiovascular and other adverse events. ^{9,10}



The data for this example were extracted from selected Data Partners contributing to the MSDD. Two of the COX-2 Inhibitors were withdrawn from the market during this period (Table 13). In addition, research conducted between January 2002 and August 2004 indicated an increased risk of cardiovascular disease events with certain COX-2 inhibitors.

COX-2 INHIBITOR	APPROVAL DATE	DATE OF WITHDRAWAL OR
		RELEASE OF ALERT
celecoxib (brand name:	12/31/1998	March 2005,FDA issued an alert
Celebrex)		that it may be associated with
		increased CVD risk
valdecoxib (brand name:	5/21/199	September 2004, withdrawn
Vioxx)		from market
valdecoxib (brand name:	11/19/2001	April 2005, withdrawn from
Bextra)		market

Table 13.	Dates of	of FDA a	pproval	and ale	t or wit	hdrawal	for COX-2	Inhibitors

2. Comparisons of Interest

a. Drug and Outcome Comparisons

In the primary analyses, we examined the association between Cox-2 Inhibitors and GI bleeding events using non-selective NSAIDs as an active comparator.

b. Methodological Comparisons

As in the simulation, we contrasted several analytic methods:

- 1. Propensity score and Disease Risk score adjustments
- 2. Matched and stratified adjustments
- 3. Two different methods of estimating the propensity and disease risk scores: 1) lookwise which used data of the current year in building score models; 2) cumulative which used data from times up to and including the current year. Although prior data is used to estimate new scores in the cumulative method, newly calculated scores are used only for the new users in a time interval for matching and stratification. Individuals who started their drugs in prior time intervals retain their original scores and matching or stratification selections.

Site specific propensity scores and disease risk scores were estimated and participants were matched or placed into strata within site. Outcome models used survival analysis and included the matching or stratification indicators as strata. Indicators for site were also included in the strata statement.

3. Data Source and Study Time Frame

We requested claims data recorded from January 2001 until December 2011 at four Data Partner sites that contributed to the MSDD: Aetna, Humana, and Kaiser Permanente in Northern California (KPNC) and Kaiser Permanente in Colorado (KPCO). Returned records showed that data were primarily available between 2008-2011 at two of the largest sites (Aetna and Humana). Thus, results in this report are restricted to that time frame. In addition, use of COX-2 inhibitors was uncommon at the smallest site



(KPCO) during this time frame and was insufficient to support site specific score estimates. Therefore, this site is not included in the primary results reported here.

4. Identification of Incident Users

We identified incident users of NSAIDs aged 18 years and older, among those who were health plan members between January 2008 and December 2011. All participants had to be enrolled in a health plan with medical and pharmacy benefits for a continuous period of six months (183 days) prior to the enrollment date (the washout period), and had no evidence of prior NSAID use. In addition, individuals with prior GI bleeding were excluded from analyses examining incident outcomes. As gaps in enrollment, pharmacy or medical benefits of 45 days or less usually represent administrative gaps rather than actual disenrollment, we ignored such gaps during participant recruitment.

We used National Drug Codes (NDCs) recorded in MSDD's outpatient pharmacy dispensing file to ascertain NSAID use. Thus, over-the-counter use was not captured. The NDCs used to identify users of COX-2 Inhibitors and Non-Selective NSAIDs in the analysis were obtained from the FirstDataBank.

5. Identification of Outcomes of Interest

Our primary outcome of interest was upper GI bleeding, including hospitalization for upper GI bleeding and Peptic Ulcer Disease. These diagnoses were identified using International Classification of Diseases, 9th Revision, Clinical Modification (ICD-9-CM) codes 531.x, 532.x, 533.x, 534.x, and 578.x^{9, 10, 11} (Table 14). The positive predictive value (PPV) for this composite algorithm is approximately 90%.^{9, 10,12,13}

Table 14. ICD-9 codes and sources for outcome of interest

OUTCOME	DEFINITION NOTES	ICD-9-CM Codes	SOURCE/NOTES
GI BLEEDING	ICD-9 discharge diagnoses	531.x, 532.x, 533.x, 534.x,	Diagnosis table and
	for hospitalization for GI	535.x, 578.x	encounter table (to
	bleeding, Peptic Ulcer		select inpatient events)
	Disease		

6. Follow-up

Analyses focused on outcomes occurring within 6 months of drug initiation. This relatively short time window was chosen for two reasons: 1) early adverse events would more likely reflect potential drug associations and 2) short-term drug use was common in this population (e.g. median time on drugs was 30 days). We followed participants from the index date until they experienced one of the following events: 1) occurrence of the outcome of interest, 2) completion of 183 days of follow-up, 3) death, 4) cessation of the use of the drug of interest or initiation of an alternative NSAID, 5) reaching the end of the study, i.e. December 31st 2011, or 6) disenrollment from the health plan.

7. Potential Confounders

Table 15 provides a list of potential confounders that we included in our analyses. We ascertained age at index date and sex from MSDD's demographic file, and current and past medical conditions during the washout period from ICD-9 diagnosis codes recorded during inpatient, outpatient, or emergency department visits from MSDD's diagnosis file.



CONFOUNDER	SOURCE/ICD-9-CM CODES
Calendar year	
Demographic Variables	
Age	MSDD demographic file
Gender	MSDD demographic file
Current or past medical conditions	
History of prior GI bleed or peptic	MSDD diagnosis file;
ulcer disease	ICD9 Codes: 530.82, 531.x, 532.x, 533.x,
	534.x, 535.x, 578.x
Modified Charlson Comorbidity	MSDD diagnosis file; see reference
Score ¹⁴	MCDD dia se a sia fila JCDO Ca da a 71.4
Rheumatold Arthritis	MSDD diagnosis file; ICD9 Codes: /14
Osteoarthritis	MSDD diagnosis file; ICD9 Codes: /15
Hypertension	MSDD diagnosis file; ICD9 Codes:401-405
History of MI	MSDD diagnosis file; ICD9 Codes:410
History of other CAD	MSDD diagnosis file: ICD9 Codes: 411-414
Diabetes	MSDD diagnosis file; ICD9 Codes:250
History of Ischemic stroke ¹¹	MSDD diagnosis file; ICD9 Codes:433,434, 436
History of non-traumatic	MSDD diagnosis file; ICD9 Codes:430 to 432
intracerebral hemorrhage	
Renal disease ¹⁴	MSDD diagnosis file: ICD9 Codes: 403.01,
	403.11,403.91, 404.02, 404.03, 404.12,
	404.13, 404.92, 404.93, 582.x, 583.0-583.7,
	585.x, 586.x, 588.0, V42.0, V45.1, V56.x
Use of Proton Pump inhibitors or	National drug codes obtained from the
H2 blockers	FirstDataBank
Use of anti-coagulant drugs	National drug codes obtained from the
	FirstDataBank

C. RESULTS

The primary analyses examining the association between COX-2 NSAID use versus non-selective NSAID comparators and GI bleed outcomes included n=2,688,965 patients with new dispensings. Table 16 shows the numbers of GI bleed outcomes within six months and the distribution of NSAID dispensings by year. GI Bleed outcomes within 6 months were rare, occurring in less than 0.2% of patients. COX-2 inhibitors accounted for less than 4% of the new NSAID dispensings in each year and use decreased slightly over the four years studied. Appendix C, Table C1 shows this same data for each of the three sites.



YEAR OF DRUG	GI BLEED WITH	IIN 6 MONTHS	TYPE OF NSAID DRUG			
INITIATION	No	Yes	Non-selective NSAID	COX-2 NSAID		
	N (%)	N (%)	N (%)	N (%)		
2008	630714	929	606495	25148		
	(99.85%)	(0.15%)	(96.02%)	(3.98%)		
2009	800308	1143	776778	24673		
	(99.86%)	(0.14%)	(96.92%)	(3.08%)		
2010	660395	889	643921	17363		
	(99.87%)	(0.13%)	(97.37%)	(2.63%)		
2011	598780	807	581236	13351		
	(99.86%)	(0.14%)	(97.75%)	(2.25%)		

Table 16. Incident GI bleed outcome numbers and COX-2 exposure numbers by year (Total N:2,688,965 excludes persons with history of GI bleed at time of NSAID initiation)

1: 4 Matched analyses (one COX-2 inhibitor matched to up to four nonselective NSAIDs)

We start by presenting results for matching based on the findings of the simulations which showed more consistent results with this method. As in the simulation, we created two matched cohorts, one with a fixed 1:1 ratio and the second with a fixed 4:1 ratio. COX-2 inhibitor use was rare and large numbers of nonselective NSAIDs were available as potential matches. Despite differing propensity score distributions, only 3 out of 80,535 COX-2 users did not have at least one match within a 0.05 caliper range and 94% had at least 4 matches within this caliper range. Table 17 presents results for both lookwise and cumulative estimated propensity score matches within ± 0.05 caliper. Results for the full cohort without this restriction are provided in Appendix C, Table 2C and those results trended slightly to the null as would be expected. In Table 17, results for the propensity scores show hazard ratios for nonselective NSAIDs versus COX-2 and the estimates are above one as would be expected given COX-2 is the referent category and these drugs are known to be protective against GI bleeding. The sequential test statistic was estimated as the parameter estimate divided by its standard error and the upper boundaries for signaling were calculated using the Lan-Demets Group Sequential approach based on the distribution of GI bleeding outcomes across the four one year time interval looks. Propensity scores estimated using lookwise versus cumulative methods showed no substantive differences and both signaled at the third look.



Table 17. Incident GI bleed outcome: results for Propensity Score matched samples (4:1) (4 Nonselective NSAIDs matched to 1 COX-2); Restricted to matches within 0.05

Look	Time ¹	Nonselecti	ive NSAID	COX-2	NSAID	HR ⁴	Sequential	Test	Signal ⁷
		GI bleeds _{cum} ²	Person years _{cum} ³	GI bleeds _{cum}	Person years _{cum}	ctive NSAID vs COX-2	test statistic ⁵	boundary ⁶	
Lookwise PS ⁸									
1	2008	264	44472	63	11510	1.17	1.119	2.1040	No
2	2009	566	88529	130	22824	1.21	1.952	2.0323	No
3	2010	769	119299	174	30701	1.23	2.391	2.0514	Yes
4	2011	932	143658	224	36877	1.15	1.813	2.0508	
Cumul	ative PS ⁹								
1	2008	271	44480	63	11510	1.22	1.412	2.1040	No
2	2009	560	88578	130	22824	1.20	1.826	2.0323	No
3	2010	750	119480	174	30702	1.19	2.071	2.0514	Yes
4	2011	918	143957	224	36878	1.12	1.456	2.0508	

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group)

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group)

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores

Table 18 presents similar results using the disease risk scores with COX-2 users matched up to four nonselective NSAID users. Similar to the propensity score matched analyses, matches were restricted to a caliper of 0.05 of the score although there were no users of COX-2 inhibitors who didn't have at least one match within this range and 99% had at least four. Appendix C, Table C3 has results with no restrictions and results were comparable though slightly moved towards the null. In Table 18, disease risk scores whether estimated by lookwise or cumulative methods both signaled at the second look.



Table 18. Incident GI bleed outcome: results for Disease Risk Score matched samples (4:1) (four Nonselective NSAIDs matched to one COX-2); Restricted to matches within 0.05

Look	Time ¹	Nonselecti	ve NSAID	COX-2	ISAID	HR ⁴	Sequential	Test	Signal ⁷
		GI bleeds _{cum} ²	Person years _{cum} ³	GI bleeds _{cum}	Person years _{cum}	ctive NSAID vs COX-2	test statistic ⁵	boundary ⁶	
Lookwise DRS ⁸									
1	2008	316	45320	63	11403	1.32	1.981	2.104	No
2	2009	663	89791	130	22602	1.32	2.848	2.0323	Yes
3	2010	889	120778	174	30366	1.33	3.376	2.0514	
4	2011	1052	144848	220	36388	1.23	2.817	2.0508	
Cumul	ative DRS	5 ⁹							
1	2008	318	45735	63	11510	1.29	1.820	2.104	No
2	2009	666	90663	130	22824	1.31	2.759	2.0323	Yes
3	2010	892	122089	174	30703	1.27	2.821	2.0514	
4	2011	1060	146772	224	36878	1.18	2.194	2.0508	

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test Statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores

1: 1 Matched analyses (one COX-2 inhibitor matched to up to four nonselective NSAIDs)

Propensity score results using a 1:1 matched sample are provided in the Appendix C, Table 4c. Analyses run with either lookwise score estimates or cumulative score estimates failed to signal at any of the four time points. In contrast, the disease risk scores matched 1:1 signaled slightly earlier than the 1:4 matched analyses (Appendix C, Table 5c). One reason for the difference in the disease risk score pattern could be related to differences in the proximity of matches for 1:1 versus 1:4 matches. Table 19 shows estimates of the differences in propensity score or disease risk scores for the 1:1 and 1:4 matched



cohorts. When the calipers were initially set, examinations of the disease risk score showed a range of near 0 up to 0.7 similar to the propensity score range of near 0 to just over 0.8. Subsequently, disease risk scores at one site were found to be problematic and the final disease risk score results removed those scores. The remaining disease risk scores were lower (maximum 0.43 and large proportion of scores < 0.01) and a smaller caliper to restrict matches further might have been useful.

Score difference	PS ¹ score: 1:1 match	PS score 4:1 match	DRS ² score 1:1 match	DRS score 4:1 match
between case and	(N=80532 COX-2)	(N=80532 COX-2)	(N=79524 COX-2)	(N=79524 COX-2)
control(s)	(N=80532 N-NSAID)	(N=234456 N-NSAID)	(N=79524 N-NSAID)	(N=317979 N-NSAID)
0	71140 (88.34%)	258308 (82.01%)	72272 (90.88%)	267048 (83.98%)
<0.001	9078 (11.27%)	50401 (16.00%)	7227 (9.09%)	50168 (15.78%)
0.001 to < 0.01	287 (0.36%)	3130 (0.99%)	22 (0.03%)	596 (0.19%)
0.01 to < 0.02	17 (0.02%)	1016 (0.32%)	3 (<0.01%)	83 (0.03%)
0.02 to < 0.03	8 (0.01%)	819 (0.26%)	0	45 (0.01%)
0.03 to < 0.04	2 (<0.01%)	700 (0.22%)	0	26 (0.01%)
0.04 to < 0.05	0	614 (0.19%)	0	13 (<0.01%)

Table 19. Differences in scores for matched san	nples (table shows estimates	from lookwise estimation)
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¹PS=propensity score; ²Disease Risk Score (scores based on results from two sites due to DRS scores problems at 1 site)

Stratification Adjusted Analyses

We explored deciles of propensity scores or disease risk scores as potential adjustments using stratified analysis. Stratified adjustment using deciles of propensity scores for the full cohort are shown in Table 20. Both lookwise and cumulative estimates of the propensity scores fail to reach a signal. Disease risk scores results similarly did not produce a significant positive test statistic (Table 21). Differing distributions of the propensity scores by COX-2 versus non-selective NSAID users are evident and are one issue in these naïve analyses (Table 22). It is typical practice to restrict propensity score analyses to subjects whose scores are in a range where more equipoise is evident. However, in this example, restricting by deciles would remove a large number of the rare outcomes (Table 23) and subsequent analyses lose power. It is less intuitive to truncate disease risk scores and such a step would obviously restrict outcome numbers as well. While it is natural to look within strata to evaluate differential risks there will be less power within strata.



Look	Time ¹	Nonselecti	ive NSAID	COX-2 M	NSAID	Adjusted HR ⁴	Sequential analysis	Test statistic	Signal ⁷
		GI bleeds _{cum} ²	Person years _{cum} ³	GI bleeds _{cum}	Person years _{cum}	Nonsele- ctive NSAID vs COX-2	test statistic ⁵	y ⁶	
Lookw	vise PS ⁸	<u> </u>	<u> </u>	<u> </u>			<u> </u>	<u> </u>	
1	2008	866	275934	63	11510	1.07	0.573	2.1040	No
2	2009	1942	628523	130	22824	1.05	0.534	2.0323	No
3	2010	2787	920050	174	30703	1.05	0.633	2.0514	No
4	2011	3544	1186492	224	36878	0.98	-0.253	2.0508	No
Cumul	ative PS ^s)							
1	2008	866	275934	63	11510	0.96	-0.277	2.1040	No
2	2009	1942	628523	130	22824	0.96	-0.499	2.0323	No
3	2010	2787	920050	174	30703	0.96	-0.540	2.0514	No
4	2011	3544	1186492	224	36878	0.89	-1.625	2.0508	No

Table 20. Incident GI bleed outcome: results for Propensity Score stratified analyses (10 strata)

Table 21. Incident GI bleed outcome: results for Disease Risk Score stratified analyses (10 strata)

Look	Time ¹	Nonselecti	ive NSAID COX-2 NSAID		HR ⁴ Nonsele-	Sequential analysis	Test statistic	Signal ⁷	
		GI bleeds _{cum} ²	Person years _{cum} ³	GI bleeds _{cum}	Person years _{cum}	ctive NSAID vs COX-2	test statistic⁵	boundary ⁶	
Lookw	ise DRS ⁸								
1	2008	813	225170	63	11403	1.05	0.403	2.1040	No
2	2009	1842	531931	130	22602	1.04	0.397	2.0323	No
3	2010	2647	781430	173	30366	1.04	0.526	2.0514	No
4	2011	3365	1005950	220	36388	0.99	-0.206.	2.0508	No



Look	Time ¹	Nonselect	ive NSAID	COX-2 NSAID		HR ⁴ Nonsele-	Sequential analysis	Test statistic	Signal ⁷
		bleeds _{cum} ²	years _{cum} ³	bleeds _{cum}	yearscum	ctive NSAID vs	test statistic⁵	bounda rv ⁶	
						COX-2		,	
Cumula	ative DRS	9							
1	2008	813	225170	63	11403	1.06	0.420	2.1040	No
2	2009	1842	531931	130	22602	1.04	0.392	2.0323	No
3	2010	2647	781430	173	30366	1.04	0.500	2.0514	No
4	2011	3365	1005950	220	36388	0.98	-0.237	2.0508	No

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test Statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores

Table 22. COX-2 and non-selection NSAID use by propensity score strata

PROPENSITY SCORE DECILES (LOOKWISE ESTIMATION)	NON-SELECTIVE NSAID	COX-2
1	241361	28102
	(9.3%)	(34.9%)
2	256151	14044
	(9.8%)	(17.4%)
3	262307	9132
	(10.1%)	(11.3%)
4	261565	6317
	(10.0%)	7.8%
5	270638	5842
	(10.4%)	(7.3%)
6	265054	4793
	(10.2%)	(6.0%)
7	263431	3999
	(10.1%)	(5.0%)
8	269597	3191
	(10.3%)	(4.0%)
9	263032	2714
	(10.1%)	(3.4%)
10	255231	2401
	(9.8%)	(3.0%)



	GI BLEED WITHIN	I 6 MONTHS
PROPENSITY SCORE DECILES (LOOKWISE ESTIMATION)	No	Yes
1	268235	1228
	(10.0%)	(32.6%)
2	269623	572
	(10.0%)	(15.2%)
3	271018	421
	(10.1%)	(11.2%)
4	267470	412
	(10.0%)	10.9%
5	276223	257
	(10.3%)	(6.8%)
6	269640	207
	(10.0%)	(5.5%)
7	267261	169
	(10.0%)	(4.5%)
8	272651	137
	(10.2%)	(3.6%)
9	265600	146
	(9.9%)	(3.9%)
10	257414	218
	(9.6%)	(5.8%)

Table 23. GI Bleed outcome by propensity score strata

IV. DISCUSSIONS

A. DISCUSSION OF SIMULATION RESULTS

Our simulation results showed that empirical power increased with higher matching ratios, whether based on propensity scores or based on disease risk scores, especially when both simulated treatments and simulated outcomes were rare. While a high matching ratio (e.g., 1:8) preserved more cases in the analytic dataset and increased empirical power, in real data applications, a higher matching ratio may not be feasible due to a limited pool of appropriate controls. For matching, we matched to the nearest score without a caliper because it would not be feasible to choose an optimal caliper for each simulated dataset in a simulation setting with different combinations of parameters. However, preliminary examination showed that the matching resulted in matched pairs with small differences between scores, particularly in rare settings.

In this simulation work, we used PS or DRS scores in stratifying current year incident users into 10 strata. In general, stratification performed less well compared to 1:4 when treatment and outcome were rare while all methods were comparable when treatment and outcome were common. This stratification approach kept all cases in the analytic datasets, but it may not be the optimal method when adjusting for confounders in sequential analyses in observational studies. Specifically, we observed that stratification based on either PS or DRS scores inflated type I error rates and empirical power, especially



when both outcomes and treatments were rare. Using this stratification approach, very different persons may be put in a stratum. Finer stratification (more strata) potentially could improve the performance of stratification as more strata more closely simulate the matching approach. Since the stratification method included all cases in the analyses, more datasets that yielded valid treatment estimates would be expected. However, that was not what we observed in early years of monitoring (Table 8). In addition, due to the limitations such as using asymptotic Lan-Demets Group Sequential approach in calculating boundaries and not considering delaying of the first analysis, further exploration of stratification is required.

In matched settings, when we had fewer, delayed looks (i.e. biennial rather than annual), there was slightly higher empirical power and type I error rates. However, changes were not large and were not evident in the stratified analyses. In analyzing real observational data, if treatments and outcomes are evenly distributed over the follow-up time, as in the simulation setting, researchers may conduct sequential analyses as scheduled given the minimal power gains with a delay. However, in analyzing real data, if there is not more information at a scheduled look, researchers may consider skipping that look until a later time when more data are available.

Instead of using individuals in the current year in the lookwise approach, our cumulative approach used data from all individuals from the beginning of monitoring to the current year to estimate PS or DRS scores. Because it includes more individuals, the cumulative approach can accommodate more confounders. In addition, cumulative methods may produce scores with less uncertainty (smaller standard error for predicted scores) due to a larger sample size. However, because the process of matching and stratification use only predicted PS/DRS scores and do not typically account for the uncertainty of these scores, the cumulative approach did not differ from the lookwise approach.¹⁵ The other reason for benefit of applying the cumulative approach not apparent in the simulation setting is that those performance measurements were averaged across 1000 replicates. Although the cumulative approach did not demonstrate an advantage here, we recommend using it in safety monitoring of emergent treatment because the lookwise approach may require exclusion of important confounders (due to non-convergence in building PS or DRS models) because of few outcomes or treatments.

We encountered non-convergence when building PS and DRS models when treatments and outcomes were rare (always) or moderately rare (sometimes). To solve this problem in a simulation setting, we chose backward covariate selection method to have the SAS codes run without manually selecting covariates for each dataset. The selection of covariates with p<0.5 to be included in the final model is the level Frank Harrell recommends.¹⁶ The primary issues relate to problems of p values being too liberal and models being 'data driven' so that they won't replicate in other settings etc. However, the goal of this simulation study is to compare different approaches in adjusting for confounders on average based on 1000 replicates NOT based on each individual dataset. Thus, we believe the use of backward selection of covariates in building PS or DRS scores is appropriate in the simulation setting.

We applied the Lan-Demets Group Sequential approach in this simulation study. This approach is an approximate, not an exact approach (i.e., the Monte Carlo approach).¹⁷ The stopping boundaries based on this approach used an asymptotic theory, which may not hold for the scenario of rare treatment and rare outcome. It may be one of the causes to inflated type I error rates in regression and stratification approaches. However, we applied the same boundaries to all approaches, yielding relative and consistent comparisons. The test statistics based on the Lan-Demets Group Sequential approach were



shown in Table A5. The trends of these test statistics supported the observations of type I error rates and empirical powers in the simulation study. Boundaries were not modified when counts of individuals and outcomes differed after score matching or stratification. We purposely calculated the upper boundaries using eligible subjects and number of cases, and then applied the same boundaries to different methods.

No changes in the ability to adjust for confounding between DRS and PS methods were observed when confounding strengths changed. We did not observe either an advantage of the DRS approach when the association of confounders with outcomes was stronger than the association with treatment or an advantage of the PS approach when the association of confounders with outcomes. The DRS approach may be less useful when there are few outcomes. Similarly, PS approach may be less useful when there are few treatments.⁴ PS has been advocated as advantageous when a single PS can be used for multiple outcomes, however disparate outcomes may require different exclusions or variable adjustments that limit duplicate use. Similarly, a single DRS model may be advantageous when studying multiple exposures but only if the population for the DRS model is appropriate for the differing exposures. Although available, methods for creating PS are not trivial when there are multiple exposures or with multiple exposure levels. In such instances, the DRS method may be advantageous because a single DRS model can be fit by including categorical variables for the exposure variable.

Invalid estimates of treatment effect were more likely due to the fact that there was no outcomes in the treatment group than in the comparator group because we set up the simulation such that the majority of the population was comparators. In calculating type I error rates, datasets with invalid estimates were considered not signaled. When treatments and outcomes were rare, the average of valid treatment effect estimates was overestimated, which was consistent with previous studies. ^{18,19,20} When treatments and outcomes were common, more datasets produced valid estimates and the average of valid estimates was unbiased.

The same information including number of subjects, number of outcomes and confounders was used for DRS and PS approaches. We did not observe significant difference between PS and DRS approaches in type I error rates and empirical powers. A limitation of this simulation study was that we did not simulate the situation where historical data could be used in building DRS model. Another limitation of this simulation study is that we did not simulate a multi-site study as in the NSAID example.

It is possible for the scenario of rare treatment and rare outcome that there is no reasonable amount of information. Another limitation is that we did not include delaying of the first analysis because of practical reasons. The SAS programs for conducting the simulation study are very complex, each containing over 9000 SAS statements. Each SAS program can generate confounders, simulate treatment status, simulate outcome, build PS and DRS models (stepwise and cumulative), perform 1:1 and 1:4 matching and stratification, and conduct sequential analyses. Inclusion of delaying the first analyses will further complicate the SAS programs and lengthen the running time of these programs which already took dozens of hours to run.

B. DISCUSSION OF THE METHODOLOGICAL EXAMPLE

The goal of comparing the risk of GI bleeding after incident use of COX-2 and nonselective NSAID drugs was to examine similar comparative methods in a data application in order to gain additional insights.



Similar to the simulation study, we did not observe meaningful differences in results when scores were created using lookwise or cumulative estimation methods. Operationally, the lookwise method has an advantage in not requiring historical data when estimating scores at later looks. Although one might expect the cumulative method to have more stable scores, neither the simulation nor the example runs displayed evidence of this potential advantage.

In comparisons of matching methods and stratification, the NSAID example agreed with the simulation results in suggesting matching as the preferred method. The example further highlighted how difficult it is to adequately adjust for confounding using stratification in a setting where scores have disparate distributions for the drug comparisons of interest.

Unlike the simulation, the NSAID example showed some differences in results for comparisons of propensity scores and disease risk scores as the disease risk score had slightly earlier or stronger signals. However, this single example does not support generalizations since the simulations would have had some runs where each score prevailed despite the overall similarities "on average". Nevertheless, the varying results on the example are helpful in highlighting several issues that will likely occur in data applications. Unlike in the simulation setting where both the propensity score models and the disease risk score models are equally correct, in real world settings we often don't know the "truth" and one score may unknowingly lack critical covariates. We can also expect the distributions of the two different scores rarely to be similar and balancing across the groups of interest will likely differ. In most applied settings, there are advantages to having both scores calculated and reviewed. If both methods signal, it will add some level of reassurance to the results. If only one method signals, additional data checks and other efforts to understand the differences will ensure a deeper understanding of any results prior to dissemination.

C. LIMITATIONS

One advantage of the disease risk score is that historical data might be available to build the model. The simulation study did not directly examine such a scenario but it is likely that results where treatments were rare but outcomes were moderate or common may reflect results that might be expected in such an instance. Another limitation is that the simulation study did not mimic the more complicated multi-site study setting that was used in the NSAID example. Nor did the simulation study use a survival outcome, but instead assumed a binary outcome without censoring. Therefore some issues of using survival outcomes should be further explored. The NSAID example was limited in not employing a variety of covariate inclusion methods (i.e. a small consistent model and a full model to be evaluated with the selected models).

V. CONCLUSION AND RECOMMENDATIONS

- This study found that stratification methods performed less well than matching methods, which is consistent with the finding reported by Austin et al (2007). ²² Matched cohort methods are preferable to stratification to adjust for potential confounders.
- 2. For rare outcomes and rare treatments, we recommend that, whenever feasible, a high matching ratio (e.g., 1:8) be used to maximize statistical power as long as matched score differences don't exceed the selected caliper estimate. For common and moderately rare



outcomes and treatments, a lower matching ratio (e.g., 1:4) is sufficient in maximizing statistical power in signaling detection.

- 3. Use both propensity score and disease risk score adjustments if possible.
- 4. Although the cumulative approach did not demonstrate an advantage here, we recommend using it in safety monitoring of emergent treatment because the lookwise approach may require exclusion of important confounders (due to non-convergence in building PS or DRS models) because of few outcomes or treatments.



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VII. APPENDIX A

			NTERCEPT		TREATMENT INTERCEPT				
	y Scenario Scenario		Scenario	Scenario	n*	Scenario	Scenario	nario Scenario	
		1	2	3		1	2	3	
Rare	<20/5000	-6.0	-6.0	-6.85	~25/5000	-6.08	-6.91	-6.08	
Moderate	~50/5000	-4.8	-4.8	-5.63	~50/5000	-5.25	-6.25	-5.40	
Common	~225-/5000	-3.3	-3.3	-4.15	>500/5000	-2.5	-3.3	-2.5	

Table A1. Intercept parameter coefficients used in simulating datasets (N=5000 in each year)

*Treatment n is for 1st look, new treatment becomes more common over time

In tables A2-A6, scenarios 1-3 represent the following

Scenario 1: Strengths of associations between confounders and exposure and confounders and outcome are the same

Scenario 2: Strength of association between confounders and exposure is greater

Scenario 3: Strength of association between confounders and outcome is greater



Table A2. Comparison of different approaches for analyzing stratified data based on propensity scores when the treatment of interest is commonly prescribed: number of datasets with valid treatment effects and mean treatment effect (standard deviation) for treatment effects θ_Z = 0.69

SCENA	θ_Z	n	y	STR	NUMBER OF DATASETS WITH VALID TREATMENT EFFECT ESTIMATES					
RIO*				ATA	AND MEAN T	REATMENT EFI	FECT (STD)		1	
					Mantel-	Firth	Conditional	Fixed	Random	
					Haenszel			effects	effect	
1	0.69	459	17	5	414	1000	946	946	946	
			Ļ		-7.16 (2.95)	1.08 (0.40)	0.65 (0.62)	0.65 (0.62)	0.67 (0.62)	
				10	96	1000	946	946	946	
			Ļ		-9.22 (2.11)	1.30 (0.31)	0.65 (0.62)	0.65 (0.62)	0.67 (0.62)	
				20	11	1000	946	946	946	
					-10.55 (1.70)	1.43 (0.26)	0.65 (0.62)	0.65 (0.62)	0.67 (0.62)	
2	0.69	463	17	5	408	1000	958	958	958	
					-7.47 (3.03)	1.28 (0.38)	0.67 (0.64)	0.67 (0.64)	0.72 (0.64)	
				10	111	1000	958	958	958	
					-9.95 (1.80)	1.39 (0.31)	0.67 (0.64)	0.67 (0.64)	0.72 (0.63)	
				20	10	1000	958	958	958	
					-11.07 (0.72)	1.50 (0.27)	0.66 (0.64)	0.67 (0.65)	0.72 (0.63)	
3	0.69	459	17	5	458	1000	949	949	949	
					-7.47 (3.16)	1.11 (0.40)	0.66 (0.63)	0.66 (0.63)	0.71 (0.63)	
				10	127	1000	949	949	949	
					-9.25 (2.34)	1.28 (0.32)	0.66 (0.63)	0.66 (0.63)	0.71 (0.63)	
				20	18	1000	949	949	958	
					-9.83 (3.29)	1.40 (0.27)	0.66 (0.63)	0.66 (0.63)	0.71 (0.63)	
1	0.69	463	109	5	999	1000	1000	1000	1000	
					-0.26 (2.01)	0.68 (0.28)	0.67 (0.27)	0.67 (0.27)	0.68 (0.27)	
				10	996	1000	1000	1000	1000	
					-3.51 (2.86)	0.73 (0.25)	0.66 (0.27)	0.67 (0.27)	0.68 (0.27)	
				20	853	1000	1000	1000	1000	
					-8.21 (2.11)	0.90 (0.20)	0.66 (0.27)	0.67 (0.27)	0.68 (0.27)	
2	0.69	463	109	5	1000	1000	1000	1000	1000	
					-1.22 (2.71)	0.70 (0.29)	0.68 (0.27)	0.68 (0.27)	0.73 (0.27)	
				10	993	1000	1000	1000	1000	
					-4.70 (2.71)	0.79 (0.25)	0.67 (0.27)	0.67 (0.27)	0.73 (0.27)	
				20	792	1000	1000	1000	1000	
					-8.74 (1.93)	0.99 (0.20)	0.67 (0.28)	0.67 (0.28)	0.73 (0.27)	
3	0.69	459	108	5	1000	1000	1000	1000	1000	
					-0.97 (2.64)	0.70 (0.29)	0.68 (0.27)	0.68 (0.27)	0.70 (0.27)	
				10	990	999	999	999	999	
					-4.49 (2.98)	0.78 (0.25)	0.68 (0.27)	0.68 (0.27)	0.70 (0.27)	
				20	825	999	999	999	999	
					-8.664 (2.02)	0.95 (0.20)	0.67 (0.27)	0.68 (0.27)	0.71 (0.27)	

 \bar{n} , mean number of the treatment of interest; \bar{y} , mean number of outcomes.


Table A3. Comparing different approaches for analyzing stratified data based on propensity scores when treatment of interest is rarely prescribed: number of datasets with valid treatment effects and mean treatment effect (standard deviation) for treatment effect θ_Z = 0.69

SCENA	θ_{Z}	n	\overline{y}	STR	NUMBER OF DATASETS WITH VALID TREATMENT EFFECT ESTIMATES					
RIO*				ATA	AND MEAN TH	REATMENT EFF	ECT (STD)			
					Mantel-	Firth	Conditional	Fixed	Random	
					Haenszel			effects	effect	
1	0.69	25	16	5	46	124	148	148	148	
					-9.07 (1.19)	3.42 (0.56)	2.67 (0.42)	2.67 (0.43)	2.67 (0.40)	
				10	10	37	148	148	148	
					-9.67 (2.19)	3.79 (2.11)	2.68 (0.45)	2.70 (0.46)	2.67 (0.40)	
				20	41	57	148	148	148	
					-8.00 (3.80)	3.29 (0.42)	2.69 (0.47)	2.73 (0.49)	2.66 (0.40)	
2	0.69	26	16	5	32	100	103	103	103	
					-8.54 (2.74)	3.26 (0.93)	2.63 (0.43)	2.64 (0.44)	2.66 (0.41)	
				10	9	13	104	103	103	
					-8.54 (3.80)	3.69 (0.28)	2.54 (1.25)	2.68 (0.53)	2.67 (0.41)	
				20	23	41	103	103	103	
					-8.49 (2.07)	3.31 (0.38)	2.63 (0.47)	2.66 (0.49)	2.65 (0.42)	
3	0.69	25	16	5	40	126	149	149	149	
					-8.85 (1.32)	3.35 (0.70)	2.64 (0.44)	2.65 (0.45)	2.63 (0.44)	
				10	34	88	149	149	149	
					-7.85 (2.40)	3.50 (0.48)	2.64 (0.45)	2.66 (0.46)	2.63 (0.44)	
				20	40	56	150	149	149	
					-8.01 (2.23)	3.25 (0.42)	2.59 (1.07)	2.70 (0.52)	2.63 (0.44)	
1	0.69	25	100	5	312	544	659	659	659	
					-8.61 (3.57)	1.82 (0.50)	1.04 (0.46)	1.04 (0.46)	1.04 (0.46)	
				10	44	79	659	659	659	
					-10.14 (1.46)	3.25 (2.22)	1.04 (0.46)	1.04 (0.47)	1.04 (0.46)	
				20	132	269	659	659	659	
					-8.25 (3.77)	1.84 (0.87)	1.04 (0.47)	1.03 (0.47)	1.04 (0.46)	
2	0.69	26	101	5	222	458	708	708	708	
					-9.27 (2.40)	2.05 (0.50)	1.00 (0.50)	1.01 (0.50)	1.06 (0.49)	
				10	60	58	708	708	708	
					-10.14(1.52)	3.03 (1.93)	1.00 (0.50)	1.00 (0.50)	1.05 (0.49)	
				20	17	0	708	708	708	
					-11.03 (0.89)		1.00 (0.51)	1.00 (0.51)	1.05 (0.49)	
3	0.69	25	100	5	319	532	649	649	649	
					-8.03 (4.11)	1.83 (0.58)	1.08 (0.49)	1.08 (0.49)	1.07 (0.49)	
				10	188	365	649	649	649	
					-6.99 (4.29)	2.17 (1.55)	1.08 (0.49)	1.08 (0.50)	1.06 (0.49)	
				20	147	254	649	649	649	
					-7.70 (3.83)	1.81 (0.82)	1.07 (0.495)	1.08 (0.50)	1.06 (0.49)	

 \bar{n} , mean number of the treatment of interest; \bar{y} , mean number of outcomes.



SCENARI	LOOK	PROPENSITY S	CORE		DISEASE RISK SCORE		
OS		Matching	Matching	Stratification	Matching	Matching	Stratification
		1:1	1:4		1:1	1:4	
1	1	4.73 (11.91)	0.02 (4.12)	-0.051 (3.23)	4.52 (11.80)	0.02 (4.14)	-0.052 (3.24)
	2	1.63 (5.60)	0.56 (1.50)	0.54 (1.32)	1.48 (5.28)	0.56 (1.50)	0.54 (1.33)
	3	0.93 (2.35)	0.67 (0.41)	0.66 (0.38)	1.07 (2.85)	0.66 (0.42)	0.65 (0.39)
	4	0.74 (0.50)	0.68 (0.32)	0.68 (0.30)	0.78 (0.52)	0.68 (0.33)	0.67 (0.30)
	5	0.73 (0.43)	0.69 (0.27)	0.68 (0.29)	0.75 (0.43)	0.68 (0.28)	0.68 (0.26)
	6	0.72 (0.37)	0.68 (0.25)	0.67 (0.24)	0.73 (0.38)	0.67 (0.25)	0.67 (0.24)
	7	0.72 (0.34)	0.68 (0.23)	0.67 (0.21)	0.73 (0.33)	0.68 (0.23)	0.68 (0.21)
	8	0.72 (0.31)	0.68 (0.21)	0.68 (0.20)	0.73 (0.30)	0.68 (0.21)	0.68 (0.20)
	9	0.71 (0.29)	0.69 (0.19)	0.68 (0.18)	0.72 (0.28)	0.69 (0.19)	0.68 (0.18)
	10	0.71 (0.27)	0.69 (0.17)	0.68 (0.17)	0.72 (0.26)	0.68 (0.18)	0.68 (0.17)
2	1	4.13 (10.95)	0.14 (3.17)	0.14 (3.17)	4.05 (10.88)	0.20 (3.42)	0.19 (2.79)
	2	1.32 (4.30)	0.64 (0.98)	0.64 (0.98)	1.79 (5.43)	0.65 (0.96)	0.65 (0.87)
	3	0.84 (1.71)	0.68 (0.40)	0.68 (0.40)	1.05 (2.84)	0.69 (0.39)	0.70 (0.37)
	4	0.73 (0.49)	0.69 (0.32)	0.68 (0.32)	0.87 (1.69)	0.70 (0.32)	0.71 (0.30)
	5	0.72 (0.41)	0.69 (0.29)	0.69 (0.29)	0.75 (0.45)	0.71 (0.28)	0.70 (0.27)
	6	0.70 (0.37)	0.69 (0.26)	0.69 (0.25)	0.73 (0.39)	0.71 (0.26)	0.70 (0.25)
	7	0.71 (0.34)	0.70 (0.23)	0.70 (0.23)	0.72 (0.33)	0.71 (0.23)	0.71 (0.22)
	8	0.70 (0.31)	0.71 (0.22)	0.71 (0.21)	0.72(0.30)	0.72 (0.21)	0.71 (0.21)
	9	0.70 (0.28)	0.71 (0.20)	0.72(0.20)	0.72 (0.28)	0.73 (0.19)	0.71 (0.19)
	10	0.70 (0.25)	0.72 (0.18)	0.72 (0.18)	0.72 (0.25)	0.73 (0.18)	0.71 (0.18)
3	1	4.78 (11.70)	0.12 (4.14)	0.02 (3.13)	4.77 (11.61)	0.07 (3.79)	0.05 (3.13)
	2	1.71 (5.45)	0.60 (1.21)	0.58 (1.07)	1.68 (5.35)	0.62 (1.21)	0.61 (1.07)
	3	0.84 (1.63)	0.66 (0.42)	0.65 (0.39)	0.93 (2.23)	0.69 (0.43)	0.68 (0.39)
	4	0.73 (0.49)	0.68 (0.33)	0.67 (0.30)	0.85 (1.60)	0.70 (0.34)	0.70 (0.30)
	5	0.73 (0.43)	0.68 (0.29)	0.68 (0.27)	0.75 (0.48)	0.71 (0.30)	0.71 (0.27)
	6	0.71 (0.37)	0.68 (0.26)	0.67 (0.24)	0.74 (0.41)	0.70 (0.27)	0.70 (0.24)
	7	0.72 (0.34)	0.68 (0.23)	0.68 (0.22)	0.74 (0.38)	0.71 (0.24)	0.70 (0.22)
	8	0.72 (0.30)	0.69 (0.21)	0.69 (0.20)	0.74 (0.33)	0.71 (0.21)	0.71 (0.20)
	9	0.71 (0.28)	0.70 (0.19)	0.69 (0.18)	0.73 (0.31)	0.72 (0.20)	0.72 (0.19)
	10	0.70 (0.26)	0.71 (0.18)	0.69 (0.18)	0.73 (0.28)	0.72 (0.19)	0.72 (0.18)

Table A4. Mean (standard deviation) of treatment effect by look with θ_z = 0.69



Table A5. Mean of test statistic by look with $\theta_z \text{=} 0.69$

SCENAR	LOOK	PROPENSITY S	SCORE		DISEASE RISK	SCORE	
IOS		Matching	Matching	Stratification	Matching	Matching	Stratification
		1:1	1:4		1:1	1:4	
1	1	0.37	0.94	1.06	0.35	0.94	1.06
	2	0.89	1.44	1.58	0.89	1.44	1.59
	3	1.18	1.78	1.93	1.21	1.76	1.94
	4	1.47	2.13	2.29	1.51	2.11	2.30
	5	1.70	2.44	2.60	1.72	2.42	2.61
	6	1.90	2.69	2.87	1.92	2.67	2.88
	7	2.12	2.98	3.15	2.13	2.96	3.17
	8	2.34	3.28	3.44	2.46	3.27	3.46
	9	2.53	3.57	3.71	2.55	3.56	3.73
	10	2.72	3.84	3.96	2.74	3.83	3.98
2	1	0.42	1.04	1.13	0.42	1.03	1.19
	2	0.92	1.52	1.63	0.94	1.53	1.73
	3	1.24	1.86	1.97	1.24	1.87	2.08
	4	1.50	2.20	2.30	1.53	2.23	2.44
	5	1.72	2.52	2.61	1.76	2.55	2.75
	6	1.91	2.81	2.87	1.96	2.85	3.04
	7	2.15	3.14	3.17	2.17	3.17	3.35
	8	2.34	3.47	3.45	2.39	3.50	3.64
	9	2.54	3.78	3.71	2.60	3.81	3.92
	10	2.75	4.07	3.94	2.80	4.10	4.17
3	1	0.37	0.96	1.09	0.36	1.00	1.14
	2	0.88	1.44	1.58	0.90	1.48	1.65
	3	1.20	1.75	1.91	1.19	1.80	2.00
	4	1.44	2.09	2.26	1.46	2.15	2.36
	5	1.68	2.41	2.59	1.70	2.49	2.71
	6	1.88	2.67	2.85	1.91	2.75	2.98
	7	2.11	2.98	3.14	2.13	3.06	3.29
	8	2.31	3.28	3.41	2.35	3.37	3.57
	9	2.49	3.60	3.69	2.56	3.69	3.85
	10	2.69	3.90	3.94	2.76	3.99	4.12



Table A6a. Rare treatment and rare outcome, lookwise estimation method, scenario 1 after increasing treatment parameter to 1.61^{*}

TREATMENT PARAMETER θ_Z =1.61 (OR=5)									
Design and	Signaled	MEAI	N $\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to				
Method	%	Signaled	Signaled and	Signal Detection	Signal Detection				
			Not, N	(STD)	(5%, 95%)				
PS Matching 1:1	8.1	2.18 (0.27)	1.35 (0.65), 746	9.59 (0.61)	10 (8 10)				
PS Matching 1:4	78.2	2.10 (0.59)	1.83 (0.77), 995	6.96 (1.90)	7 (4 10)				
PS Stratification	90.3	2.10 (0.63)	1.96 (0.74), 998	4.10 (2.70)	3 (1 9)				
DRS Matching 1:1	8.1	2.22 (0.26)	1.35 (0.68), 743	9.48 (0.71)	10 (8 10)				
DRS Matching 1:4	78.4	2.10 (0.60)	1.82 (0.78), 996	6.96 (1.94)	7 (4 10)				
DRS Stratification	90.4	2.10 (0.63)	1.97 (0.74), 998	4.10 (2.70)	3 (1 9)				

*Description of the columns in Tables6a-6c, see the second paragraph of Appendix B.

Table A6b. Rare treatment rare outcome, lookwise estimation method, scenario 2 after increasingtreatment parameter to 1.61

TREATMENT PARAMETER θ_Z =1.61 (OR=5)									
Design and	Signaled	MEAI	N $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to				
Method	%	Signaled	Signaled Signaled and		Signal Detection				
			Not, N	(STD)	(5%, 95%)				
PS Matching 1:1	0.5	1.34 (0.05)	1.03 (0.67), 504	10 (NA)	10 (10, 10)				
PS Matching 1:4	46.5	2.24 (0.53)	1.71 (0.80), 893	7.96 (1.68)	8 (5 10)				
PS Stratification	77.3	2.33 (0.70)	2.07 (0.88), 924	4.51 (2.95)	4 (1 10)				
DRS Matching 1:1	0.5	2.08 (0.35)	1.05 (0.65), 534	10 (NA)	10 (10, 10)				
DRS Matching 1:4	46.6	2.27 (0.53)	1.72 (0.81), 889	8.00 (1.75)	8 (5 10)				
DRS Stratification	76.8	2.32 (0.69)	2.06 (0.88), 924	4.48 (2.97)	4 (1 10)				

Table A6c. Rare treatment rare outcome, lookwise estimation method, scenario 3 after increasingtreatment parameter to 1.61

TREATMENT PARAMETER θ_Z =1.61 (OR=5)										
Design and	Signaled	MEA	N $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to					
Method	%	Signaled	Signaled and	Signal Detection	Signal Detection					
			Not, N	(STD)	(5%, 95%)					
PS Matching 1:1	0.3	2.13 (0.29)	0.91 (0.71), 517	9.67 (0.58)	10 (9 10)					
PS Matching 1:4	45.9	2.29 (0.51)	1.68 (0.84), 931	8.02 (1.67)	8 (5 10)					
PS Stratification	77.9	2.39 (0.73)	2.06 (0.95), 974	4.44 (3.01)	4 (1 10)					
DRS Matching 1:1	0.2	2.30 (NA)	0.93 (0.70), 513	9.00 (NA)	9 (9 9)					
DRS Matching 1:4	44.9	2.34 (0.52)	1.70 (0.85), 927	8.11 (1.63)	8 (5 10)					
DRS Stratification	78.3	2.39 (0.73)	2.07 (0.95), 974	4.43 (3.01)	4 (1 10)					



VIII. APPENDIX B

This appendix provides results from all simulations that were performed on an annual basis for a period of ten years. The treatment parameter is set to 0 and 0.69. In the tables below, "lookwise estimation method" and "cumulative estimation method" refer to the method for creating PS model and DRS model in the sequential analyses (Section II, 6a and 6b). "Scenario 1", "scenario 2", and "scenario 3" refer to different scenarios in which the strengths of associations between confounders $x_1 - x_4$ and exposure and confounders $x_1 - x_4$ and outcome differ (Table 1).

Description of the columns:

Type 1 error %: Percentage of false positives when the treatment parameter is set to 0. Signaled %: Empirical power when the treatment parameter is set to 0.69.

Signaled: Average treatment parameter obtained from signaled replicates when the treatment parameter is set to 0.69.

Signaled and not: Average parameter obtained from signaled replicates and those that did not signal at the end of follow-up (only datasets that converged were included) when the treatment parameter is set to 0.69.

N = Number of replicate data sets that converged i.e., the number that was used to calculate the average parameter

We included all variables listed in Table 1 to compute PSs and DRSs used in these analyses with the exception of scenarios in which either the treatment or outcome was rare or moderately rare. In order to ensure that the models converged, we used a backward selection method (p<0.5) in these scenarios to limit the number of variables included.

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	θ_Z =0	Signaled	MEAN	$\hat{ heta}_{Z}$ (STD)	Mean Time to	Median Time to	
Method	(OR=1)	%			Signal Detection	Signal Detection	
	Type 1		Signaled	Signaled	(STD)	(5% <i>,</i> 95%)	
	Error %			and Not, N			
PS Matching	0.0	0.0	NA	0.40 (0.71),	NA	NA	
1:1				712			
PS Matching	2.0	14.7	1.94	0.74 (0.80),	8.19 (1.68)	8 (5 10)	
1:4			(0.48)	929			
PS	10.4	36.4	1.91	0.93 (0.96),	4.95 (3.15)	5 (1 10)	
Stratification			(0.66)	932			
DRS Matching	0.0	0.0	NA	0.44 (0.75),	NA	NA	
1:1				711			
DRS Matching	1.6	13.3	1.94	0.73 (0.78),	8.11 (1.70)	8 (5 10)	
1:4			(0.45)	930			
DRS	10.1	36.0	1.93	0.93 (0.96),	4.84 (3.13)	4 (1 10)	
Stratification			(0.66)	929			

Table B1-1.	Rare treatment and	rare outcome.	lookwise estimation	method, and	l scenario 1
TADIC DI-I.	a naic ti catilicitti alla	rare outcome,	lookwise estimation	method, and	a section in



		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to	
Method	(OR=1)	%			Signal	Signal Detection	
	Type 1		Signaled	Signaled	Detection (STD)	(5%, 95%)	
	Error %			and Not, N			
PS Matching	0	0.0	NA	0.23 (0.63),	NA	NA	
1:1				711			
PS Matching	0.9	5.1	2.19	0.85 (0.77),	8.67 (1.70)	9 (5 10)	
1:4			(0.48)	799			
PS	11	30.6	2.24	1.14 (1.01),	4.86 (3.29)	5 (1 10)	
Stratification			(0.76)	818			
DRS Matching	0	0.0	NA	0.22 (0.62),	NA	NA	
1:1				569			
DRS Matching	0.8	4.7	2.18	0.84 (0.79),	8.70 (1.63)	9 (6 10)	
1:4			(0.44)	805			
DRS	10.7	30.6	2.25	1.14 (1.02),	4.82 (3.32)	5 (1 10)	
Stratification			(0.75)	818			

Table B1-2. Rare treatment and rare outcome, lookwise estimation method, and scenario

Table B1-3. Rare treatment and rare outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and Method	θ _Z =0 (OR=1)	Signaled %	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to Signal	Median Time to Signal Detection	
	Type 1 Error %		Signaled	Signaled and Not, N	Detection (STD)	(5%, 95%)	
PS Matching 1:1	0	0.0	NA	0.19 (0.60), 528	NA	NA	
PS Matching 1:4	1.0	5.8	2.30 (0.45)	0.92 (0.81), 762	8.52 (1.50)	9 (6 10)	
PS Stratification	10.9	30.8	2.38 (0.77)	1.26 (1.06), 784	4.45 (3.19)	4 (1 10)	
DRS Matching 1:1	0	0.0	NA	0.22 (0.57), 526	NA	NA	
DRS Matching 1:4	0.5	5.7	2.29 (0.45)	0.92 (0.80), 755	8.42 (1.69)	9 (5 10)	
DRS Stratification	11.6	31.0	2.37 (0.75)	1.27 (1.05), 783	4.40 (3.17)	4 (1 10)	



TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{\theta}_{z}$ (STD)		Mean Time to	Median Time to		
Method	(OR=1)	%			Signal	Signal Detection		
	Type 1		Signaled	Signaled	Detection	(5%, 95%)		
	Error %			and Not, N	(STD)			
PS Matching	0	0.1	2.30 (NA)	0.40 (0.75),	9.0 (NA)	9.0 (NA)		
1:1				714				
PS Matching	1.7	14.9	2.01	0.75 (0.82),	8.05 (1.70)	8 (5 10)		
1:4			(0.50)	932				
PS	9.9	35.8	1.93	0.93 (0.96),	4.84 (3.09)	4 (1 10)		
Stratification			(0.66)	932				
DRS Matching	0	0.1	2.30 (NA)	0.36 (0.74),	9.0 (NA)	9.0 (NA)		
1:1				724				
DRS Matching	1.7	14.8	1.92	0.73 (0.80),	8.34 (1.63)	8.5 (5 10)		
1:4			(0.46)	928				
DRS	10.7	36.0	1.93	0.94 (0.96),	4.78 (3.10)	4 (1 10)		
Stratification			(0.66)	932				
regression	10	35.9	1.93	1.50 (0.78),	4.81 (3.08)	4 (1 10)		
			(0.67)	572				

Table B1-4. Rare treatment and rare outcome, cumulative estimation method, and scenario 1

Table B1-5. Rare treatment and rare outcome, cumulative estimation method, and scenario 2

TREATMENT PARAMETER θ_Z =0.69 (OR=2)									
Design and	θ_Z =0	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to			
Method	(OR=1)	%			Signal	Signal Detection			
	Type 1		Signaled	Signaled	Detection	(5%, 95%)			
	Error %			and Not, N	(STD)				
PS Matching	0	0	NA	0.23 (0.62),	NA	NA			
1:1				536					
PS Matching	0.6	5.5	2.31	0.84 (0.76),	8.84 (1.71)	9 (4 10)			
1:4			(0.49)	802					
PS	11.1	30.3	2.25	1.13 (1.01),	4.87 (3.30)	5 (1 10)			
Stratification			(0.78)	818					
DRS Matching	0	0	NA	0.22 (0.63),	NA	NA			
1:1				553					
DRS Matching	0.7	4.9	2.13	0.86 (0.78),	8.61 (1.51)	9 (6 10)			
1:4			(0.46)	792					
DRS	10.9	31.0	2.24	1.15 (1.01),	4.87 (3.34)	5 (1 10)			
Stratification			(0.75)	818					
regression	10.2	28.7	2.25	1.66 (0.89),	4.80 (3.24)	5 (1 10)			
			(0.77)	507					



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	θ_Z =0	Signaled	MEAN	$\hat{ heta}_{Z}$ (STD)	Mean Time to	Median Time to			
Method	(OR=1)	%		_	Signal Detection	Signal Detection			
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)			
	Error %			and Not, N					
PS Matching	0	0	NA	0.26 (0.58),	NA	NA			
1:1				496					
PS Matching	0.5	6.6	2.24	0.94 (0.79),	8.41 (1.68)	9 (5 10)			
1:4			(0.47)	758					
PS	11.3	31.0	2.38	1.27 (1.05),	4.41 (3.17)	4 (1 10)			
Stratification			(0.77)	785					
DRS Matching	0	0	NA	0.22 (0.60),	NA	NA			
1:1				515					
DRS Matching	0.7	6.3	2.23	0.92 (0.81),	8.67 (1.51)	9 (6 10)			
1:4			(0.51)	759					
DRS	11.5	30.9	2.37	1.24 (1.13),	4.45 (3.20)	4 (1 10)			
Stratification			(0.75)	786					
regression	10.9	30.1	2.35	1.84 (0.92),	4.56 (3.20)	4 (1 10)			
			(0.78)	474					

Table B1-6. Rare treatment and rare outcome, cumulative estimation method, and scenario 3

Table B2-1. Rare treatment and moderate outcome, lookwise estimation method, and scenario 1

	TREATMENT PARAMETER θ_Z =0.69 (OR=2)						
Design and Method	θ _Z =0 (OR=1)	Signaled %	MEAN	$\widehat{ heta}_{Z}$ (STD)	Mean Time to Signal	Median Time to Signal Detection	
	Type 1 Error %		Signaled	Signaled and Not, N	Detection (STD)	(5%, 95%)	
PS Matching 1:1	0.0	1.0	2.26 (0.32)	0.68 (0.73), 921	9.50 (0.53)	9.50 (9, 10)	
PS Matching 1:4	3.8	28.2	1.75 (0.55)	0.79 (0.79), 993	7.19 (2.05)	7 (3, 10)	
PS Stratification	8.7	44.8	1.57 (0.54)	0.88 (0.79), 993	5.18 (2.95)	5 (1, 10)	
DRS Matching 1:1	0.0	1.3	2.06 (0.37)	0.72 (0.74), 912	9.69 (0.48)	10 (9, 10)	
DRS Matching 1:4	4.6	30.9	1.72 (0.50)	0.82 (0.77), 992	7.18 (1.97)	7 (3, 10)	
DRS Stratification	9.0	45.2	1.58 (0.55)	0.89 (0.79), 993	5.13 (2.94)	5 (1 10)	



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	θ_Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to			
Method	(OR=1)	%		-	Signal	Signal Detection			
	Type 1		Signaled	Signaled	Detection (STD)	(5%, 95%)			
	Error %			and Not, N					
PS Matching	0	2.1	2.11	0.74 (0.72),	9.33 (0.80)	10 (8, 10)			
1:1			(0.31)	929					
PS Matching	4.3	28.8	1.68	0.81 (0.72),	7.03 (2.11)	7 (3, 10)			
1:4			(0.50)	995					
PS	8.7	47.4	1.51	0.91 (0.73),	5.40 (2.97)	5 (1, 10)			
Stratification			(0.52)	995					
DRS Matching	0	2.0	2.15	0.71 (0.71),	9.60 (0.60)	10 (8.5, 10)			
1:1			(0.33)	917					
DRS Matching	4.1	30.4	1.69	0.82 (0.73),	7.23 (2.10)	7 (4, 10)			
1:4			(0.49)	995					
DRS	9.3	49.4	1.51	0.93 (0.74),	5.44 (2.98)	6 (1, 10)			
Stratification			(0.52)	995					

Table B2-2. Rare treatment and moderate outcome, lookwise estimation method, and scenario2

Table B2-3. Rare treatment and moderate outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and Method	θ _Z =0 (OR=1)	Signaled %	MEAN	$\hat{ heta}_Z$ (STD)	Mean Time to Signal	Median Time to Signal Detection	
	Type 1 Error %		Signaled	Signaled and Not, N	Detection (STD)	(5%, 95%)	
PS Matching 1:1	0	1.4	2.19 (0.29)	0.68 (0.75), 929	9.71 (0.61)	10 (8, 10)	
PS Matching 1:4	3.9	30.3	1.67(0.51)	0.79 (0.77), 997	7.16 (2.12)	7 (3, 10)	
PS Stratification	10.5	48.5	1.53 (0.53)	0.89 (0.79), 997	5.28 (2.85)	6 (1, 10)	
DRS Matching 1:1	0	1.5	2.13 (0.29)	0.69 (0.78), 915	9.67 (0.49)	10 (9, 10)	
DRS Matching 1:4	3.8	30.8	1.69 (0.52)	0.80 (0.78), 997	7.21 (2.07)	7 (3, 10)	
DRS Stratification	10.1	49.1	1.53 (0.52)	0.90 (0.79), 997	5.27 (2.84)	5 (1, 10)	



TREATMENT PARAMETER θ_Z =0.69 (OR=2)										
Design and	θ_Z =0 (OR=1)	Signaled	MEA	AN $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to				
Method	Type 1 Error %	%	Signaled	Signaled and	Signal	Signal Detection				
				Not, N	Detection (STD)	(5%, 95%)				
PS Matching	0.0	1.6	2.16	0.72 (0.77), 911	9.38 (0.62)	9.00 (8, 10)				
1:1			(0.28)							
PS Matching	3.8	28.9	1.75	0.80 (0.79), 993	7.16 (2.02)	7 (3, 10)				
1:4			(0.53)							
PS	8.7	44.8	1.57	0.88 (0.79), 993	5.21 (2.93)	5 (1, 10)				
Stratification			(0.55)							
DRS	0.0	1.7	2.15	0.69 (0.75), 907	9.41 (0.62)	9 (8, 10)				
Matching 1:1			(0.29)							
DRS	4.1	29.9	1.72	0.81 (0.77), 993	7.37 (1.99)	8 (4, 10)				
Matching 1:4			(0.53)							
DRS	9.4	46.0	1.58	0.90 (0.79), 993	5.18 (2.91)	5 (1, 10)				
Stratification			(0.55)							
Regression	8.7	44.9	1.57	0.87 (0.89), 994	5.16 (2.96)	5 (1, 10)				
			(0.55)							

Table B2-4. Rare treatment and moderate outcome, cumulative estimation method, scenario 1

Table B2-5. Rare treatment and moderate outcome, cumulative estimation method, and scenario2

TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	θ_Z =0 (OR=1)	Signaled	MEA	NN $\hat{ heta}_{Z}$ (STD)	Mean Time to	Median Time to	
Method	Type 1 Error %	%	Signaled	Signaled and	Signal	Signal Detection	
				Not, N	Detection (STD)	(5%, 95%)	
PS Matching	0	1.6	2.16	0.73 (0.71), 923	9.31 (0.87)	10 (8, 10)	
1:1			(0.32)				
PS Matching	4.4	28.3	1.68	0.80 (0.75), 995	7.17 (2.02)	8 (3, 10)	
1:4			(0.50)				
PS	8.3	45.4	1.51	0.88 (0.74), 995	5.37 (2.98)	5 (1, 10)	
Stratification			(0.53)				
DRS	0	2.3	2.15	0.77 (0.72), 910	9.43 (0.73)	10 (8, 10)	
Matching 1:1			(0.29)				
DRS	3.9	29.0	1.74	0.85 (0.75), 995	7.10 (2.05)	7 (3, 10)	
Matching 1:4			(0.53)				
DRS	9.6	49.4	1.52	0.94 (0.74), 995	5.38 (2.95)	6 (1, 10)	
Stratification			(0.52)				
Regression	7.8	45.7	1.51	0.87 (0.84), 996	5.36 (3.00)	5 (1, 10)	
			(0.53)				



TREATMENT PARAMETER θ_Z =0.69 (OR=2)									
Design and	θ_Z =0 (OR=1)	Signaled	MEA	N $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to			
Method	Type 1 Error	%	Signaled	Signaled and	Signal	Signal Detection			
	%			Not, N	Detection	(5%, 95%)			
					(STD)				
PS Matching	0	1.6	2.08 (0.31)	0.67 (0.76), 923	9.75 (0.58)	10 (8, 10)			
1:1									
PS Matching	4.5	30.0	1.70 (0.54)	0.78 (0.79), 997	7.16 (2.06)	7 (3, 10)			
1:4									
PS	10.2	47.0	1.54 (0.54)	0.87 (0.80), 997	5.28 (2.89)	5 (1, 10)			
Stratification									
DRS Matching	0.1	1.6	1.99 (0.33)	0.69 (0.75), 938	9.75 (0.45)	10 (9, 10)			
1:1									
DRS Matching	4.7	30.3	1.74 (0.54)	0.80 (0.80), 997	7.10 (2.12)	7 (3, 10)			
1:4									
DRS	9.9	47.4	1.54 (0.53)	0.89 (0.79), 997	5.24 (2.85)	5 (1, 10)			
Stratification									
Regression	10.1	46.4	1.54 (0.56)	0.83 (1.06),	5.23 (2.91)	5 (1, 10)			
				1000					

Table B2-6. Rare treatment and moderate outcome, cumulative estimation method, and scenario 3

Table B3-1. Rare treatment and common outcome, lookwise estimation method, and scenario 1

	TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	θ_Z =0 (OR=1)	Signaled	MEA	N $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to		
Method	Type 1 Error %	%	Signaled	Signaled and Not, N	Signal Detection (STD)	Signal Detection (5%, 95%)		
PS Matching 1:1	1.6	42.0	1.29 (0.44)	0.81 (0.53),1000	7.70 (1.67)	8 (5 10)		
PS Matching 1:4	5.6	72.6	1.03 (0.41)	0.85 (0.47),1000	6.18 (2.52)	6 (2 10)		
PS Stratification	7.9	82.7	0.99 (0.39)	0.87 (0.43),1000	5.24 (2.76)	5 (1 10)		
DRS Matching 1:1	1.6	48.2	1.30 (0.45)	0.86 (0.56),1000	7.70 (1.63)	8 (5 10)		
DRS Matching 1:4	5.0	73.3	1.08 (0.44)	0.89 (0.50), 1000	5.95 (2.48)	6 (2 10)		
DRS Stratification	8.4	83.7	0.99 (0.38)	0.88 (0.43), 1000	5.23 (2.74)	5 (1, 10)		



TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	θ_Z =0 (OR=1)	Signaled	MEAN	$\hat{ heta}_{Z}$ (STD)	Mean Time to	Median Time to		
Method	Type 1 Error	%	Signaled	Signaled and	Signal	Signal Detection		
	%			Not, N	Detection	(5%, 95%)		
					(STD)			
PS Matching	2.2	45.2	1.31 (0.44)	0.84	7.68 (1.66)	8 (5 10)		
1:1				(0.55),1000				
PS Matching	5.7	74.0	1.11 (0.47)	0.92	5.86 (2.53)	6 (2 10)		
1:4				(0.52),1000				
PS	9.4	84.9	1.03 (0.39)	0.93	4.91 (2.70)	5 (1 10)		
Stratification				(0.44),999				
DRS	1.6	47.7	1.34 (0.46)	0.89	7.58 (1.70)	8 (5 10)		
Matching 1:1				(0.56),1000				
DRS	2.2	75.4	1.12 (0.48)	0.94	5.84 (2.54)	6 (2 10)		
Matching 1:4				(0.53),1000				
DRS	3.8	86.3	1.04 (0.39)	0.95	4.86 (2.65)	5 (1 9)		
Stratification				(0.44),1000				

Table B3-2. Rare treatment and common outcome, lookwise estimation method, and scenario 2

Table B3-3: Rare treatment and common outcome, lookwise estimation method, and scenario 3

	TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	θ_Z =0 (OR=1)	Signaled	MEAI	N $\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to		
Method	Type 1 Error %	%	Signaled	Signaled and Not, N	Signal Detection (STD)	Signal Detection (5%, 95%)		
PS Matching	2.2	45.8	1.30	0.84	7.47 (1.68)	7.5 (5 10)		
1:1			(0.42)	(0.54),1000				
PS Matching	5.9	74.9	1.08	0.91	5.87 (2.54)	6 (2 10)		
1:4			(0.44)	(0.50),1000				
PS	8.2	86.2	1.00	0.91	5.11 (2.72)	5 (1 10)		
Stratification			(0.39)	(0.43),1000				
DRS Matching	3.2	48.1	1.29	0.86	7.50 (1.70)	7 (5 10)		
1:1			(0.42)	(0.53),1000				
DRS Matching	5.4	76.4	1.08	0.91	5.85 (2.52)	6 (2 10)		
1:4			(0.44)	(0.49),1000				
DRS	8.6	86.1	1.00	0.91	5.13 (2.71)	5 (1 10)		
Stratification			(0.40)	(0.44),1000				



TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{\theta}_z$ (STD)		Mean Time to	Median Time to		
Method	(OR=1)	%			Signal Detection	Signal Detection		
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)		
	Error %			and Not, N				
PS Matching	1.7	44.4	1.29	0.83	7.72 (1.67)	8 (5 10)		
1:1			(0.43)	(0.53),1000				
PS Matching	5.9	72.7	1.07	0.89	5.97 (2.48)	6 (2 10)		
1:4			(0.44)	(0.39),1000				
PS	8.1	83.5	0.99	0.88	5.25 (2.76)	5 (1 10)		
Stratification			(0.38)	(0.43),1000				
DRS Matching	3.0	46.7	1.34	0.87	7.59 (1.67)	8 (5 10)		
1:1			(0.44)	(0.56),1000				
DRS Matching	6.2	73.0	1.07	0.88	6.03 (2.51)	6 (2 10)		
1:4			(0.44)	(0.50),1000				
DRS	8.8	83.6	0.99	0.88	5.23 (2.76)	5 (1 10)		
Stratification			(0.39)	(0.43),1000				
regression	7.8	82.8	0.98	0.87	5.29 (2.77)	5 (1 10)		
			(0.39)	(0.44),1000				

Table B3-4. Rare treatment and common outcome, cumulative estimation method, and scenario 1

Table B3-5. Rare treatment and common outcome, cumulative estimation method, and scenario 2

	TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	θ_Z =0	Signaled	MEAN	$\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to		
Method	(OR=1)	%			Signal Detection	Signal Detection		
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)		
	Error %			and Not, N				
PS Matching	2.3	45.5	1.33	0.87 (0.55),	7.57 (1.71)	8 (5 10)		
1:1			(0.43)	1000				
PS Matching	6.5	75.3	1.10	0.92 (0.51),	5.89 (2.53)	6 (2 10)		
1:4			(0.46)	1000				
PS	9.5	84.6	1.03	0.92 (0.44),	4.92 (2.70)	5 (1 10)		
Stratification			(0.39)	1000				
DRS Matching	2.4	47.3	1.32	0.88 (0.54),	7.64 (1.75)	8 (5 10)		
1:1			(0.44)	1000				
DRS Matching	5.4	75.6	1.13	0.95 (0.53),	5.78 (2.56)	6 (2 10)		
1:4			(0.48)	1000				
DRS	10.4	85.7	1.04	0.94 (0.44),	4.87 (2.68)	5 (1 9)		
Stratification			(0.39)	1000				
regression	8.4	82.9	1.00	0.89 (0.44),	5.10 (2.73)	5 (1 10)		
			(0.39)	1000				



TREATMENT PARAMETER θ_z =0.69 (OR=2)							
Design and	θ_Z =0	Signaled	MEAN $\widehat{ heta}_Z$ (STD)		Mean Time to	Median Time to	
Method	(OR=1)	%		•	Signal Detection	Signal Detection	
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)	
	Error %			and Not, N			
PS Matching	1.8	48.2	1.29	0.86 (0.54),	7.57 (1.74)	8 (5 10)	
1:1			(0.44)	1000			
PS Matching	7.1	77.5	1.07	0.92 (0.49),	5.91 (2.52)	6 (2 10)	
1:4			(0.43)	1000			
PS	9.4	87.2	1.00	0.92 (0.43),	5.09 (2.69)	5 (1 10)	
Stratification			(0.39)	1000			
DRS Matching	3.2	48.2	1.32	0.88 (0.55),	7.44 (1.68)	7 (5 10)	
1:1			(0.43)	1000			
DRS Matching	5.4	76.4	1.08	0.91 (0.49),	5.91 (2.55)	6 (2 10)	
1:4			(0.44)	1000			
DRS	8.2	85.9	1.00	0.91 (0.44),	5.13 (2.72)	5 (1 10)	
Stratification			(0.39)	1000			
regression	7.2	84.5	1.00	0.89 (0.45),	5.18 (2.74)	5 (1 10)	
			(0.40)	1000			

Table B3-6. Rare treatment and common outcome, cumulative estimation method, and scenario 3

Table B4-1. Moderate treatment and rare outcome, lookwise estimation method, and scenario 1

		TREATME	NT PARAMET	ER θ_Z =0.69 (O	R=2)	
Design and	θ _Z =0	Signaled	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to	Median Time to
Method	(OR=1)	%		-	Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	0	0.7	2.16	0.60 (0.75),	8.86 (0.38)	10 (9 10)
1:1			(032)	872		
PS Matching	2.8	24.8	1.76	0.74 (0.79),	7.62 (2.08)	8 (4 10)
1:4			(0.51)	989		
PS	9.0	39.7	1.62	0.82 (0.82),	5.26 (2.96)	5 (1 10)
Stratification			(0.55)	989		
DRS Matching	0	0.6	2.23	0.58 (0.77),	9.83 (0.41)	10 (9 10)
1:1			(0.26)	881		
DRS Matching	3.1	24.3	1.82	0.72 (0.83),	7.52 (2.04)	8 (4 10)
1:4			(0.54)	988		
DRS	9.2	38.9	a.62 (0.54)	0.81 (0.82),	5.22 (2.92)	5 (1 10)
Stratification				988		



TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to	
Method	(OR=1)	%			Signal Detection	Signal Detection	
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)	
	Error %			and Not, N			
PS Matching	0	1.5	2.08	0.69 (0.76),	9.33 (1.05)	10 (7 10)	
1:1			(0.32)	915			
PS Matching	3.4	30.6	1.73	0.81 (0.79),	7.23 (2.02)	7 (4 10)	
1:4			(0.55)	995			
PS	8.6	44.4	1.54	0.88 (0.76),	5.19 (2.90)	5 (1 10)	
Stratification			(0.53)	995			
DRS Matching	0	1.5	2.06	0.70 (0.76),	9.20 (0.86)	9 (8 10)	
1:1			(0.39)	928			
DRS Matching	3.5	29.7	1.74	0.81 (0.78),	7.08 (2.02)	7 (4 10)	
1:4			(0.52)	995			
DRS	8.6	44.2	1.54	0.87 (0.76),	5.21 (2.90)	5 (1 10)	
Stratification			(0.52)	995			

Table B4-2. Moderate treatment-rare outcome, lookwise estimation method, and scenario 2

Table B4-3. Moderate treatment and rare outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2			=2)	
Design and	$\theta_Z=0$	signaled	MEAN $\hat{\theta}_Z$ (STD)			Median Time to
Method	(OR=1)	%		P		Signal Detection
	Type 1		Signaled	Signaled	Mean Time To	(5%, 95%)
	Error %			and Not, N	Signal Detection	
					(STD)	
PS Matching	0	0.8	2.10 (0.40)	0.67 (0.75),	9.63 (0.74)	10 (8 10)
1:1				912		
PS Matching	3.7	28.1	1.76 (0.54)	0.81 (0.78),	7.22 (2.08)	8 (4 10)
1:4				992		
PS	9.0	46.6	1.54 (0.52)	0.90 (0.77),	5.23 (2.93)	5 (1 10)
Stratification				992		
DRS Matching	0	0.7	2.17 (0.32)	0.65 (0.75),	9.57 (0.79)	10 (8 10)
1:1				904		
DRS Matching	3.8	27.3	1.76 (0.55)	0.79 (0.78),	7.15 (2.13)	7 (3 10)
1:4				992		
DRS	8.1	45.1	1.56 (0.53)	0.89 (0.77),	5.26 (2.93)	5 (1 10)
Stratification				992		



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Table B4-4. Moderate treatment and rare outcome, cumulative estimation method, and scenario 1

Table B4-5. Moderate treatment and rare outcome, cumulative estimation method, and scenario 2

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{\theta}_{Z}$ (STD)		Mean Time to	Median Time to
Method	(OR=1)	%			Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	0	1.4	2.23	0.69 (0.76),	9.36 (1.08)	10 (7 10)
1:1			(0.26)	922		
PS Matching	2.6	29.2	1.68	0.78 (0.76),	7.27 (1.98)	8 (4 10)
1:4			(0.51)	995		
PS	7.5	44.4	1.53	0.87 (0.76),	5.24 (2.92)	5 (1 10)
Stratification			(0.53)	995		
DRS Matching	0	1.7	2.14	0.70 (0.74),	9.41 (0.94)	10 (7 10)
1:1			(0.30)	916		
DRS Matching	2.9	2.90	1.76	0.81 (0.78),	7.03 (2.08)	7 (4 10)
1:4			(0.53)	995		
DRS	7.5	45.0	1.53	0.88 (0.76),	5.31 (2.92)	5 (1 10)
Stratification			(0.53)	995		
regression	6.8	43.7	1.51	1.05 (0.71),	5.35 (2.94)	5 (1 10)
			(0.52)	784		



TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and	θ_Z =0	Signaled	MEAN $\widehat{ heta}_Z$ (STD)		Mean Time to	Median Time to	
Method	(OR=1)	%		1	Signal Detection	Signal Detection	
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)	
	Error %			and Not, N			
PS Matching	0	0.8	2.20	0.66 (0.75),	9.12 (0.83)	9 (8 10)	
1:1			(0.31)	906			
PS Matching	4.3	28.5	1.72	0.80 (0.76),	7.28 (2.05)	8 (4 10)	
1:4			(0.50)	992			
PS	8.6	46.1	1.55	0.90 (0.77),	5.28 (2.92)	5 (1 10)	
Stratification			(0.52)	992			
DRS Matching	0	1.2	2.19	0.67 (0.76),	9.67 (0.65)	10 (8 10)	
1:1			(0.36)	904			
DRS Matching	3.7	27.6	1.74	0.78 (0.78),	7.29 (2.11)	8 (3 10)	
1:4			(0.53)	992			
DRS	8.4	45.2	1.55	0.88 (0.77),	5.24 (2.91)	5 (1 10)	
Stratification			(0.53)	992			
regression	7.7	43.0	1.55	1.07 (0.73),	5.31 (2.95)	5 (1 10)	
			(0.54)	777			

Table B4-6. Moderate treatment and rare outcome, cumulative estimation method, and scenario 3

Table B5-1. Moderate treatment and moderate outcome, lookwise estimation method, and scenario 1

		TREATME	NT PARAMET	ER θ_Z =0.69 (O	R=2)	
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to	Median Time to
Method	(OR=1)	%		1	Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	0.7	19.7	1.77	0.83 (0.64),	8.70 (1.14)	9 (7 10)
1:1			(0.43)	997		
PS Matching	5.8	50.9	1.39	0.90 (0.66),	6.31 (2.41)	6 (2 10)
1:4			(0.55)	1000		
PS	8.6	65.7	1.24	0.92 (0.59),	5.21 (2.96)	5 (1 10)
Stratification			(0.45)	1000		
DRS	0.5	17.2	1.76	0.79 (0.64),	8.67 (1.22)	9 (7 10)
Matching 1:1			(0.43)	992		
DRS	5.2	49.6	1.37	0.88 (0.66),	6.40 (2.45)	7 (3 10)
Matching 1:4			(0.54)	1000		
DRS	8.8	65.9	1.24	0.93 (0.59),	5.24 (2.97)	5 (1 10)
Stratification			(0.46)	1000		



TREATMENT PARAMETER θ_z =0.69 (OR=2)							
Design and	θ_Z =0	Signaled	MEAN $\hat{\theta}_z$ (STD)		Mean Time to	Median Time to	
Method	(OR=1)	%			Signal Detection	Signal Detection	
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)	
	Error %			and Not, N			
PS Matching	0.7	16.9	1.79	0.83 (0.65),	8.82 (1.07)	9 (7 10)	
1:1			(0.39)	993			
PS Matching	5.9	49.4	1.43	0.91	6.33 (2.43)	6 (3 10)	
1:4			(0.54)	(0.67),1000			
PS	9.7	66.8	1.28	0.97	5.16 (3.02)	5 (1 10)	
Stratification			(0.48)	(0.61),1000			
DRS	0.8	16.1	1.83	0.83 (0.65),	8.71 (1.22)	9 (7 10)	
Matching 1:1			(0.44)	995			
DRS	6.8	50.9	1.38	0.91	6.54 (2.45)	7 (2 10)	
Matching 1:4			(0.52)	(0.64),1000			
DRS	9.9	67.5	1.28	0.98	5.17 (2.99)	5 (1 10)	
Stratification			(0.48)	(0.61),1000			

Table B5-2. Moderate treatment and moderate outcome, lookwise estimation method, and scenario 2

Table B5-3. Moderate treatment and moderate outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to	Median Time to
Method	(OR=1)	%		1	Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	0.2	15.8	1.79	0.80 (0.66),	8.86 (1.11)	9 (7 10)
1:1			(0.44)	995		
PS Matching	4.5	50.0	1.40	0.89	6.46 (2.43)	7 (2.5 10)
1:4			(0.51)	(0.66),1000		
PS	8.5	65.4	1.28	0.96	5.06 (2.86)	5 (1 10)
Stratification			(0.46)	(0.60),1000		
DRS	0.2	16.1	1.84	0.80 (0.67),	8.83 (1.12)	9 (7 10)
Matching 1:1			(0.44)	998		
DRS	4.5	50.9	1.37	0.89	6.55 (2.38)	7 (2 10)
Matching 1:4			(0.50)	(0.65),1000		
DRS	8.4	65.2	1.27	0.95	5.13 (2.86)	5 (1 10)
Stratification			(0.46)	(0.60),1000		



		TREATME	NT PARAMET	ER θ_Z =0.69 (O	R=2)	
Design and Method	θ _Z =0 (OR=1)	Signaled %	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to Signal Detection	Median Time to Signal Detection
	Type 1 Error %		Signaled	Signaled and Not, N	(STD)	(5%, 95%)
PS Matching 1:1	0.6	18.3	1.73 (0.45)	0.79 (0.63),999	8.72 (1.20)	9 (7 10)
PS Matching 1:4	5.0	50.3	1.37 (0.51)	0.89 (0.64),1000	6.32 (2.47)	6 (2 10)
PS Stratification	8.7	65.7	1.24 (0.45)	0.92 (0.59),1000	5.20 (2.95)	5 (1 10)
DRS Matching 1:1	0.6	17.7	1.80 (0.46)	0.80 (0.65),996	8.74 (1.21)	9 (7 10)
DRS Matching 1:4	5.7	49.1	1.39 (0.54)	0.88 (0.66),1000	6.32 (2.47)	7 (2 10)
DRS Stratification	8.8	65.6	1.24 (0.46)	0.93 (0.59),999	5.20 (2.96)	5 (1 10)
regression	8.4	65.1	1.24 (0.46)	1.03 (0.54),883	5.20 (2.96)	5 (1 10)

Table B5-4. Moderate treatment and moderate outcome, cumulative estimation method, andscenario 1

Table B5-5: Moderate treatment and moderate outcome, cumulative estimation method, and scenario 2

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	θ_Z =0	Signaled	MEAN $\hat{\theta}_z$ (STD)		Mean Time to	Median Time to
Method	(OR=1)	%			Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	0.6	15.5	1.83	0.81	8.72 (1.14)	9 (7 10)
1:1			(0.42)	(0.68),994		
PS Matching	4.7	50.4	1.39	0.90	6.46 (2.49)	7 (2 10)
1:4			(0.52)	(0.65),1000		
PS	9.8	66.2	1.29	0.96	5.12 (3.02)	5 (1 10)
Stratification			(0.48)	(0.61),1000		
DRS Matching	0.6	16.2	1.85	0.83	8.65 (1.17)	9 (7 10)
1:1			(0.45)	(0.66),987		
DRS Matching	6.4	50.5	1.42	0.92	6.46 (2.44)	7 (2 10)
1:4			(0.57)	(0.68),1000		
DRS	10.3	67.4	1.28	0.98	5.13 (2.97)	5 (1 10)
Stratification			(0.48)	(0.61),1000		
regression	8.9	64.2	1.27	1.04	5.17 (3.00)	5 (1 10)
			(0.48)	(0.56),895		



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)							
Design and Mothod	$\theta_Z = 0$	Signaled	MEAN	$\hat{ heta}_Z$ (STD)	Mean Time to	Median Time to		
Wethou	Type 1	70	Signaled	Signaled	(STD)	(5%, 95%)		
	Error %		-	and Not, N				
PS Matching	0.5	16.1	1.79	0.81 (0.65),	8.86 (1.13)	9 (7 10)		
1:1			(0.45)	997				
PS Matching	4.9	50.3	1.40	0.89	6.43 (2.43)	6 (3 10)		
1:4			(0.52)	(0.67),1000				
PS	8.9	65.6	1.28	0.96	5.08 (2.85)	5 (1 10)		
Stratification			(0.46)	(0.60),1000				
DRS Matching	0.3	17.0	1.83	0.79	8.88 (1.08)	9 (7 10)		
1:1			(0.43)	(0.68),994				
DRS Matching	5.2	50.5	1.41	0.90	6.47 (2.47)	7 (2 10)		
1:4			(0.53)	(0.67),1000				
DRS	8.7	63.9	1.28	0.94	5.05 (2.82)	5 (1 10)		
Stratification			(0.46)	(0.61),1000				
regression	7.8	61.9	1.27	1.02	5.15 (2.90)	5 (1 10)		
			(0.46)	(0.55),883				

Table B5-6. Moderate treatment and moderate outcome, cumulative estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	<i>θ</i> _Z =0	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to
Method	(OR=1)	%			Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	4.2	77.4	1.06	0.91 (0.49),	6.49 (2.20)	6 (3 10)
1:1			(0.45)	1000		
PS Matching	6.2	93.4	0.93	0.89 (0.43),	4.86 (2.38)	5 (1 9)
1:4			(0.41)	1000		
PS	8.2	97.6	0.87	0.86 (0.33),	4.14 (2.34)	4 (1 9)
Stratification			(0.32)	1000		
DRS	2.8	78.0	1.06	0.91 (0.50),	6.54 (2.14)	7 (3 10)
Matching 1:1			(0.47)	1000		
DRS	6.8	94.0	0.95	0.91 (0.43),	4.77 (2.40)	4 (1 9)
Matching 1:4			(0.41)	1000		
DRS	6.8	97.0	0.88	0.86 (0.34),	4.11 (2.30)	4 (1 9)
Stratification			(0.32)	1000		



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	θ_Z =0	Signaled	MEAN $\hat{\theta}_z$ (STD)		Mean Time to	Median Time to			
Method	(OR=1)	%			Signal Detection	Signal Detection			
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)			
	Error %			and Not, N					
PS Matching	4.8	89.0	0.98	0.92 (0.48),	5.94 (2.30)	6 (3 10)			
1:1			(0.46)	1000					
PS Matching	8.8	97.6	0.93	0.92 (0.43),	4.11 (2.23)	4 (1 9)			
1:4			(0.43)	1000					
PS	9.4	99.4	0.86	0.86 (0.31),	3.44 (1.99)	3 (1 7)			
Stratification			(0.30)	1000					
DRS	6.2	91.6	0.99	0.94 (0.47),	5.86 (2.19)	6 (3 10)			
Matching 1:1			(0.46)	1000					
DRS	10.0	98.0	0.92	0.91 (0.40),	4.11 (2.16)	4 (1 8)			
Matching 1:4			(0.39)	1000					
DRS	10.8	99.4	0.89	0.89 (0.31),	3.30 (1.92)	3 (1 7)			
Stratification			(0.30)	1000					

Table B6-2. Moderate treatment and common outcome, lookwise estimation method, and scenario 2

Table B6-3. Moderate treatment and common outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	<i>θ</i> _Z =0	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to
Method	(OR=1)	%		-	Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	4.4	83.2	1.02	0.92 (0.46),	6.18 (2.14)	6 (3 10)
1:1			(0.43)	1000		
PS Matching	7.4	98.0	0.94	0.93 (0.47),	4.68 (2.40)	4 (1 9)
1:4			(0.47)	1000		
PS	11.4	99.2	0.89	0.89 (0.32),	3.75 (2.14)	3 (1 8)
Stratification			(0.32)	1000		
DRS	4.2	82.6	1.05	0.93 (0.49),	6.15 (2.12)	6 (3 10)
Matching 1:1			(0.46)	1000		
DRS	8.0	97.0	0.94	0.92 (0.40),	4.48 (2.21)	4 (1 8)
Matching 1:4			(0.40)	1000		
DRS	10.6	99.0	0.89	0.88 (0.33),	3.79 (2.19)	3 (1 7)
Stratification			(0.32)	1000		



Table B6-4. Moderate treatment and common outcome, cumulative estimation method, and scenario1

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	θ_Z =0	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to
Method	(OR=1)	%			Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	2.8	76.6	1.06	0.91 (0.48),	6.47 (2.15)	6 (3 10)
1:1			(0.44)	1000		
PS Matching	6.4	94.0	0.94	0.90 (0.42),	4.86 (2.37)	5 (1 9)
1:4			(0.40)	1000		
PS	8.0	96.8	0.87	0.85 (0.34),	4.10 (2.29)	4 (1 9)
Stratification			(0.33)	1000		
DRS	4.0	76.8	1.07	0.91 (0.49),	6.38 (2.06)	6 (3 10)
Matching 1:1			(0.44)	1000		
DRS	7.2	92.4	0.96	0.91 (0.44),	4.78 (2.46)	4 (1 9)
Matching 1:4			(0.42)	1000		
DRS	7.8	97.0	0.87	0.86 (0.34),	4.10 (2.28)	4 (18)
Stratification			(0.32)	1000		
regression	8.0	96.4	0.87	0.85 (0.34),	4.13 (2.31)	4 (1 9)
			(0.33)	1000		

Table B6-5. Moderate treatment and common outcome, cumulative estimation method, and scenario2

	TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	<i>θ</i> _Z =0	Signaled	MEAN	$\hat{\theta}_{Z}$ (STD)	Mean Time to	Median Time to
Method	(OR=1)	%			Signal Detection	Signal Detection
	Type 1		Signaled	Signaled	(STD)	(5%, 95%)
	Error %			and Not, N		
PS Matching	4.4	90.8	0.99	0.93 (0.46),	5.87 (2.21)	6 (3 10)
1:1			(0.44)	1000		
PS Matching	8.8	97.4	0.94	0.93 (0.43),	4.10 (2.25)	4 (1 8)
1:4			(0.43)	1000		
PS	8.8	99.4	0.86	0.86 (0.31),	3.47 (2.02)	3 (1 7)
Stratification			(0.30)	1000		
DRS	5.8	91.8	0.97	0.92 (0.43),	5.88 (2.16)	6 (3 10)
Matching 1:1			(0.41)	1000		
DRS	8.0	97.8	0.93	0.91 (0.40),	4.08 (2.18)	4 (1 9)
Matching 1:4			(0.39)	1000		
DRS	10.0	99.4	0.88	0.88 (0.31),	3.34 (1.96)	3 (1 7)
Stratification			(0.31)	1000		
regression	7.8	99.2	0.84	0.84 (0.31),	3.60 (2.10)	3 (1 8)
			(0.30)	1000		



Table B6-6. Moderate treatment and common outcome, cumulative estimation method, and scenario3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	<i>θ</i> _Z =0	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to Signal	
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	4.0	83.2	1.02 (0.43)	0.91 (0.46),	6.26 (2.17)	6 (3 10)	
1:1				1000			
PS Matching	7.6	97.6	0.94 (0.44)	0.92 (0.45),	4.61 (2.35)	4 (1 9)	
1:4				1000			
PS	11.0	99.2	0.90 (0.32)	0.89 (0.32),	3.72 (2.11)	3 (1 8)	
Stratification				1000			
DRS	2.8	82.6	1.01 (0.42)	0.90 (0.45),	6.20 (2.09)	6 (3 10)	
Matching 1:1				998			
DRS	7.2	97.6	0.93 (0.39)	0.92 (0.39),	4.56 (2.33)	4 (1 9)	
Matching 1:4				998			
DRS	10.6	98.8	0.88 (0.32)	0.88 (0.33),	3.80 (2.19)	4 (1 8)	
Stratification				998			
regression	8.6	98.8	0.87 (0.33)	0.86 (0.33),	3.95 (2.25)	4 (1 8)	
				998			

Table B7-1. Common treatment and rare outcome, lookwise estimation method, and scenario 1

		TREATME				
Design and Method	θ _Z =0 (OR=1)	Signaled %	MEAN	$\hat{ heta}_{Z}$ (STD)	Mean Time to Signal Detection	Median Time to Signal Detection (5%, 95%)
	Type 1 Error %		Signaled	Signaled and Not, N	(STD)	
PS Matching 1:1	3.7	78.6	1.04 (0.42)	0.89 (0.47), 1000	6.24 (2.15)	6 (3 10)
PS Matching 1:4	6.7	95.5	0.95 (0.44)	0.92 (0.45), 1000	4.56 (2.43)	4 (1 9)
PS Stratification	7.7	96.2	0.91 (0.37)	1.05 (0.46), 1000	4.22 (2.49)	4 (1 9)
DRS Matching 1:1	3.0	79.1	1.05 (0.46)	0.91 (0.50), 996	6.27 (2.21)	6 (3 10)
DRS Matching 1:4	6.6	95.7	0.93 (0.42)	0.91 (0.43), 996	4.64 (2.44)	4 (1 9)
DRS Stratification	7.9	95.8	0.91 (0.36)	0.89 (0.37), 995	4.19 (2.48)	4 (1 9)



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{\theta}_{z}$ (STD)		Mean Time to	Median Time to Signal			
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)			
	Type 1		Signaled	Signaled and	(STD)				
	Error %			Not, N					
PS Matching	2.5	81.1	1.00 (0.42)	0.88 (0.46),	6.29 (2.20)	6 (3 10)			
1:1				1000					
PS Matching	7.1	96.7	0.92 (0.40)	0.90 (0.41),	4.56 (2.42)	4 (1 9)			
1:4				1000					
PS	6.6	95.7	0.91 (0.37)	0.88 (0.38),	4.26 (2.47)	4 (1 9)			
Stratification				1000					
DRS Matching	2.9	80.1	1.04 (0.45)	0.90 (0.49),	6.21 (2.21)	6 (3 10)			
1:1				1000					
DRS Matching	8.7	96.7	0.94 (0.41)	0.92 (0.42),	4.44 (2.36)	4 (1 9)			
1:4				1000					
DRS	7.5	96.6	0.92 (0.36)	0.90 (0.38),	4.05 (2.40)	4 (1 9)			
Stratification				1000					

Table B7-2. Common treatment and rare outcome, lookwise estimation method, and scenario 2

Table B7-3. Common treatment and rare outcome, lookwise estimation method, and scenario 3

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)				
Design and	$\theta_Z = 0$	Signaled	MEAN	$\widehat{ heta}_Z$ (STD)	Mean Time to	Median Time to Signal
Wethou	(UK-1) Type 1	70	Signaled	Signaled and	(STD)	Detection (5%, 55%)
	Error %		Signaleu	Not, N	(012)	
PS Matching 1:1	2.5	76.4	1.04 (0.42)	0.88 (0.47), 1000	6.22 (2.17)	6 (3 10)
PS Matching 1:4	6.2	95.5	0.94 (0.41)	0.91 (0.42), 1000	4.65 (2.46)	4 (1 9)
PS Stratification	6.1	95.9	0.92 (0.36)	0.89 (0.37), 1000	4.21 (2.45)	4 (1 9)
DRS Matching 1:1	3.5	78.8	1.06 (0.44)	0.90 (0.48), 1000	6.23 (2.15)	6 (3 10)
DRS Matching 1:4	5.9	96.3	0.98 (0.46)	0.95 (0.47), 1000	4.48 (2.46)	4 (1 9)
DRS Stratification	7.4	96.6	0.94 (0.37)	0.92 (0.38), 1000	4.04 (2.39)	4 (1 9)



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)								
Design and	θ_Z =0	Signaled	MEAN $\hat{\theta}_z$ (STD)		Mean Time to	Median Time to Signal			
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)			
	Type 1		Signaled	Signaled and	(STD)				
	Error %			Not, N					
PS Matching	2.9	79.2	1.03 (0.41)	0.89 (0.45),	6.32 (2.15)	6 (3 10)			
1:1				1000					
PS Matching	6.3	95.4	0.94 (0.44)	0.91 (0.45),	4.58 (2.45)	4 (1 9)			
1:4				1000					
PS	7.9	96.3	0.91 (0.37)	0.89 (0.38),	4.22 (2.49)	4 (1 9)			
Stratification				1000					
DRS Matching	3.2	78.7	1.05 (0.46)	0.91 (0.49),	6.31 (2.17)	6 (3 10)			
1:1				1000					
DRS Matching	6.7	96.2	0.93 (0.42)	0.90 (0.43),	4.62 (2.43)	4 (1 9)			
1:4				1000					
DRS	8.1	96.7	0.91 (0.36)	0.89 (0.37),	4.21 (2.49)	4 (1 9)			
Stratification				1000					
Regression	7.1	96.5	0.91 (0.36)	0.89 (0.37),	4.23 (2.47)	4 (1 9)			
				999					

Table B7-4. Common treatment and rare outcome, lookwise estimation method, and scenario 3

Table B7-5. Common treatment and rare outcome, cumulative estimation method, and scenario 2

		TREATME	NT PARAMET	ER θ_Z =0.69 (OR	=2)	
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\widehat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)
	Type 1		Signaled	Signaled and	(STD)	
	Error %			Not, N		
PS Matching	3.6	80.8	1.01 (0.44)	0.89 (0.47),	6.33 (2.17)	6 (3 10)
1:1				1000		
PS Matching	7.3	96.9	0.92 (0.40)	0.90 (0.41),	4.56 (2.38)	4 (1 9)
1:4				1000		
PS	6.8	95.7	0.91 (0.37)	0.88 (0.38),	4.25 (2.46)	4 (1 9)
Stratification				1000		
DRS Matching	3.4	82.4	1.05 (0.46)	0.93 (0.50),	6.15 (2.17)	6 (3 10)
1:1				1000		
DRS Matching	8.7	97.9	0.94 (0.42)	0.92 (0.43),	4.50 (2.40)	4 (1 9)
1:4				1000		
DRS	8.4	97.4	0.93 (0.36)	0.92 (0.37),	4.01 (2.37)	4 (1 9)
Stratification				1000		
Regression	6.5	95.8	0.89 (0.35)	0.87 (0.36),	4.26 (2.43)	4 (1 9)
				999		



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)										
Design and	θ_Z =0	Signaled	MEAN $\hat{\theta}_{Z}$ (STD)		Mean Time to		Median Time to Signal				
Method	(OR=1)	%			Signal	Detection	Detection (5%, 95%)				
	Type 1		Signaled	Signaled and	(STD)						
	Error %			Not, N							
PS Matching	3.4	77.7	1.02 (0.41)	0.89	6.34	(2.25)	6 (3 10)				
1:1				(0.45), 998							
PS Matching	6.4	95.9	0.93	0.91	4.69	(2.46)	4 (1 9)				
1:4			0.43	(0.43), 998							
PS	6.4	96.3	0.91	0.89	4.37	(2.53)	4 (1 9)				
Stratification			0.36	(0.37), 998							
DRS Matching	3.8	79.9	1.06	0.92	6.16	(2.10)	6 (3 10)				
1:1			0.41	(0.46), 996							
DRS Matching	7.8	95.9	0.97	0.95	4.54	(2.44)	4 (1 9)				
1:4			0.48	(0.48), 996							
DRS	8.2	96.8	0.93	0.91	4.11	(2.40)	4 (1 9)				
Stratification			0.36	(0.37), 996							
Regression	6.0	96.1	0.90	0.88	4.35	(2.52)	4 (1 9)				
			0.35	(0.37), 998							

Table B7-6. Common treatment and rare outcome, cumulative estimation method, and scenario 3

Table B8-1. Common treatment and moderate outcome, lookwise estimation method, and scenario 1

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%	-	r	Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	4.7	99.8	0.90 (0.40)	0.90 (0.40),	3.55 (1.65)	3 (1, 7)	
1:1				1000			
PS Matching	6.5	100	0.81 (0.26)	0.81 (0.26),	2.34 (1.25)	2 (1, 5)	
1:4				1000			
PS	6.6	100	0.79 (0.23)	0.79 (0.23),	2.11 (1.11)	2 (1, 4)	
Stratification				1000			
DRS Matching	4.4	100	0.88 (0.36)	0.88 (0.36),	3.58 (1.67)	3 (1, 7)	
1:1				1000			
DRS Matching	7.8	100	0.82 (0.26)	0.82 (0.26),	2.33 (1.23)	2 (1, 5)	
1:4				1000			
DRS	7.6	100	0.79 (0.23)	0.79 (0.23),	2.11 (1.13)	2 (1 4)	
Stratification				1000			



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)									
Design and	θ_Z =0	Signaled	MEAN	$\hat{\theta}_{Z}$ (STD)	Mean Time to	Median Time to Signal				
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)				
	Type 1		Signaled	Signaled and	(STD)					
	Error %			Not, N						
PS Matching	3.8	100	0.88 (0.39)	0.88 (0.39),	3.45 (1.64)	3 (1, 7)				
1:1				1000						
PS Matching	9.2	100	0.82 (0.25)	0.82 (0.25),	2.26 (1.19)	2 (1, 4)				
1:4				1000						
PS	6.2	100	0.80 (0.23)	0.80 (0.23),	2.10 (1.14)	2 (1, 4)				
Stratification				1000						
DRS Matching	7.2	99.9	0.91 (0.40)	0.91 (0.40),	3.37 (1.64)	3 (1, 7)				
1:1				1000						
DRS Matching	12.2	100	0.84 (0.26)	0.83 (0.26),	2.22 (1.18)	2 (1, 4)				
1:4				1000						
DRS	11.2	100	0.82 (0.23)	0.82 (0.23),	1.98 (1.07)	2 (1, 4)				
Stratification				1000						

Table B8-2. Common treatment and moderate outcome, lookwise estimation method, and scenario 2

Table B8-3. Common treatment and moderate outcome, lookwise estimation method, and scenario 3

		TREATME	NT PARAMET	ER θ_Z =0.69 (OR:	=2)		
Design and Method	$\theta_Z = 0$	Signaled %	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Methou	Type 1	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching 1:1	5.3	100	0.93 (0.40)	0.93 (0.40), 1000	3.26 (1.57)	3 (1, 6)	
PS Matching	8.6	100	0.85 (0.27)	0.85 (0.27),	2.14 (1.11)	2 (1, 4)	
1.4	0.1	100	0.04 (0.22)	1000	1.00.(0.00)	2(1, 4)	
PS Stratification	8.1	100	0.84 (0.23)	0.83 (0.23), 1000	1.88 (0.96)	2 (1, 4)	
DRS Matching 1:1	6.4	100	0.89 (0.39)	0.89 (0.39), 1000	3.42 (1.55)	3 (1, 6)	
DRS Matching	11.1	100	0.83 (0.26)	0.83 (0.26),	2.19 (1.12)	2 (1, 4)	
1:4				1000			
DRS Stratification	11.2	100	0.82 (0.23)	0.82 (0.23), 1000	1.94 (1.00)	2 (1, 4)	



Table B8-4. Common treatment and moderate outcome, cumulative estimation method, and scenario1

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	θ_Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	4.7	99.9	0.88 (0.40)	0.88 (0.40),	3.64 (1.68)	3 (1, 7)	
1:1				1000			
PS Matching	6.5	100	0.81 (0.26)	0.81 (0.26),	2.37 (1.29)	2 (1, 5)	
1:4				1000			
PS	6.6	100	0.78 (0.23)	0.78 (0.23),	2.15 (1.15)	2 (1, 4)	
Stratification				1000			
DRS Matching	4.4	99.9	0.89 (0.39)	0.88 (0.39),	3.56 (1.69)	3 (1, 7)	
1:1				1000			
DRS Matching	7.8	100	0.82 (0.26)	0.82 (0.26),	2.33 (1.22)	2 (1, 5)	
1:4				1000			
DRS	7.6	100	0.79 (0.23)	0.79 (0.23),	2.09 (1.12)	2 (1, 4)	
Stratification				1000			
regression	6.8	100	0.78 (0.23)	0.78 (0.23),	2.15 (1.14)	2 (1, 4)	
				1000			

Table B8-5. Common treatment and moderate outcome, cumulative estimation method, and scenario2

		TREATME	ATMENT PARAMETER $ heta_Z$ =0.69 (OR=2)			
Design and	θ_Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)
	Type 1		Signaled	Signaled and	(STD)	
	Error %			Not, N		
PS Matching	3.8	99.9	0.88 (0.41)	0.88 (0.41),	3.53 (1.69)	3 (1, 7)
1:1				1000		
PS Matching	9.2	100	0.81 (0.26)	0.81 (0.26),	2.30 (1.23)	2 (1, 5)
1:4				1000		
PS	6.2	100	0.79 (0.23)	0.79 (0.23),	2.17 (1.17)	2 (1, 4)
Stratification				1000		
DRS Matching	7.2	99.9	0.92 (0.40)	0.92 (0.40),	3.36 (1.65)	3 (1, 7)
1:1				1000		
DRS Matching	12.2	100	0.84 (0.26)	0.84 (0.26),	2.17 (1.14)	2 (1, 4)
1:4				1000		
DRS	11.2	100	0.83 (0.23)	0.83 (0.23),	1.95 (1.03)	2 (1, 4)
Stratification				1000		
regression	6.2	100	0.79 (0.23)	0.79 (0.23),	2.18 (1.19)	2 (1, 4)
				1000		



Table B8-6. Common treatment and moderate outcome, cumulative estimation method, and scenario3

		TREATMENT PARAMETER $ heta_Z$ =0.69 (OR=2)					
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	5.3	100	0.86 (0.38)	0.86 (0.38),	3.50 (1.64)	3 (1, 6)	
1:1				1000			
PS Matching	8.6	100	0.81 (0.26)	0.81 (0.26),	2.28 (1.24)	2 (1, 5)	
1:4				1000			
PS	8.1	100	0.79 (0.23)	0.79 (0.23),	2.05 (1.10)	2 (1, 4)	
Stratification				1000			
DRS Matching	6.4	100	0.90 (0.40)	0.90 (0.40),	3.36 (1.58)	3 (1, 6)	
1:1				1000			
DRS Matching	11.1	100	0.84 (0.27)	0.84 (0.27),	2.17 (1.12)	2 (1, 4)	
1:4				1000			
DRS	11.2	100	0.83 (0.23)	0.83 (0.23),	1.92 (1.01)	2 (1, 4)	
Stratification				1000			
regression	7.9	100	0.79 (0.23)	0.79 (0.23),	2.09 (1.14)	1 (1, 4)	
				1000			

Table B9-1. Common treatment and common outcome, lookwise estimation method, and scenario 1

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	<i>θ</i> _Z =0	Signaled	MEAN $\hat{\theta}_{Z}$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%		•	Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	5.8	100	0.76 (0.22)	0.76 (0.22),	1.55 (0.67)	1 (1, 3)	
1:1				1000			
PS Matching	5.6	100	0.70 (0.16)	0.70 (0.16),	1.16 (0.37)	1 (1, 2)	
1:4				1000			
PS	5.5	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.32)	1 (1, 2)	
Stratification				1000			
DRS Matching	6.3	100	0.77 (0.22)	0.77 (0.22),	1.50 (0.62)	1 (1, 3)	
1:1				1000			
DRS Matching	6.3	100	0.71 (0.16)	0.71 (0.16),	1.15 (0.36)	1 (1, 2)	
1:4				1000			
DRS	6.8	100	0.70 (0.15)	0.70 (0.15),	1.10 (0.32)	1 (1, 2)	
Stratification				1000			



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)									
Design and	θ_Z =0	Signaled	MEAN $\hat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal				
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)				
	Type 1		Signaled	Signaled and	(STD)					
	Error %			Not, N						
PS Matching	5.5	100	0.75 (0.22)	0.75 (0.22),	1.50 (0.63)	1 (1, 3)				
1:1				1000						
PS Matching	11.0	100	0.71 (0.16)	0.71 (0.16),	1.15 (0.39)	1 (1, 2)				
1:4				1000						
PS	5.0	100	0.70 (0.15)	0.70 (0.15),	1.12 (0.35)	1 (1, 2)				
Stratification				1000						
DRS Matching	11.4	100	0.81 (0.23)	0.81 (0.23),	1.38 (0.56)	1 (1, 2)				
1:1				1000						
DRS Matching	17.8	100	0.76 (0.17)	0.76 (0.17),	1.11 (0.33)	1 (1, 2)				
1:4				1000						
DRS	18.1	100	0.74 (0.16)	0.74 (0.16),	1.07 (0.27)	1 (1, 2)				
Stratification				1000						

Table B9-2. Common treatment and common outcome, lookwise estimation method, and scenario 2

Table B9-3. Common treatment and common outcome, lookwise estimation method, and scenario 3

		TREATME	NT PARAMET	ER θ_Z =0.69 (OR:	=2)		
Design and	$\theta_Z = 0$	Signaled	MEAN $\hat{\theta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	2.2	100	0.74 (0.22)	0.74 (0.22),	1.57 (0.66)	1 (1, 3)	
1:1				1000			
PS Matching	3.4	100	0.69 (0.16)	0.69 (0.16),	1.19 (0.40)	1 (1, 2)	
1:4				1000			
PS	2.9	100	0.68 (0.15)	0.68 (0.15),	1.14 (0.35)	1 (1, 2)	
Stratification				1000			
DRS Matching	3.7	100	0.78 (0.22)	0.78 (0.22),	1.47 (0.62)	1 (1, 3)	
1:1				1000			
DRS Matching	5.3	100	0.71 (0.17)	0.71 (0.17),	1.17 (0.39)	1 (1, 2)	
1:4				1000			
DRS	4.4	100	0.71 (0.16)	0.71 (0.16),	1.12 (0.32)	1 (1, 2)	
Stratification				1000			



	TREATMENT PARAMETER θ_Z =0.69 (OR=2)									
Design and	θ_Z =0	Signaled	MEAN $\hat{ heta}_{Z}$ (STD)		Mean Time to	Median Time to Signal				
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)				
	Type 1		Signaled	Signaled and	(STD)					
	Error %			Not, N						
PS Matching	5.4	100	0.75 (0.22)	0.75 (0.22),	1.56 (0.69)	1 (1, 3)				
1:1				1000						
PS Matching	5.9	100	0.70 (0.16)	0.70 (0.16),	1.16 (0.37)	1 (1,2)				
1:4				1000						
PS	5.1	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.32)	1 (1,2)				
Stratification				1000						
DRS Matching	5.7	100	0.77 (0.22)	0.77 (0.22),	1.50 (0.62)	1 (1,2)				
1:1				1000						
DRS Matching	6.5	100	0.71 (0.16)	0.71 (0.16),	1.15 (0.37)	1 (1,2)				
1:4				1000						
DRS	6.8	100	0.70 (0.15)	0.70 (0.15),	1.10 (0.30)	1 (1,2)				
Stratification				1000						
Regression	5.0	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.32)	1 (1,2)				
				1000						

Table B9-4. Common treatment and common outcome, cumulative estimation method, and scenario 1

Table B9-5. Common treatment and common outcome, cumulative estimation method, and scenario 2

		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	$\theta_Z = 0$	Signaled	MEAN $\widehat{ heta}_Z$ (STD)		Mean Time to	Median Time to Signal	
Method	(OR=1)	%		I	Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled and	(STD)		
	Error %			Not, N			
PS Matching	4.7	100	0.75 (0.21)	0.75 (0.21),	1.49 (0.64)	1 (1,3)	
1:1				1000			
PS Matching	10.3	100	0.71 (0.15)	0.71 (0.15),	1.14 (0.37)	1 (1,2)	
1:4				1000			
PS	6.0	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.33)	1 (1,2)	
Stratification				1000			
DRS Matching	11.2	100	0.81 (0.23)	0.81 (0.23),	1.40 (0.58)	1 (1,2)	
1:1				1000			
DRS Matching	17.0	100	0.75 (0.16)	0.75 (0.16),	1.11 (0.32)	1 (1,2)	
1:4				1000			
DRS	15.3	100	0.74 (0.16)	0.74 (0.16),	1.07 (0.25)	1 (1,2)	
Stratification				1000			
Regression	5.2	100	0.70 (0.15)	0.70 (0.15),	1.12 (0.34)	1 (1,2)	
				1000			



		TREATMENT PARAMETER θ_Z =0.69 (OR=2)					
Design and	θ_Z =0	Signaled	MEAN	$\hat{\theta}_{Z}$ (STD)	Mean Time to	Median Time to Signal	
Method	(OR=1)	%			Signal Detection	Detection (5%, 95%)	
	Type 1		Signaled	Signaled Signaled and (ST			
	Error %			Not, N			
PS Matching	5.7	100	0.75 (0.22)	0.75 (0.22),	1.56 (0.69)	1 (1,3)	
1:1				1000			
PS Matching	8.3	100	0.70 (0.16)	0.70 (0.16),	1.16 (0.38)	1 (1,2)	
1:4				1000			
PS	6.6	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.32)	1 (1,2)	
Stratification				1000			
DRS Matching	8.0	100	0.78 (0.22)	0.78 (0.22),	1.47 (0.62)	1 (1,3)	
1:1				1000			
DRS Matching	10.9	100	0.72 (0.16)	0.72 (0.16),	1.13 (0.35)	1 (1,2)	
1:4				1000			
DRS	10.8	100	0.72 (0.15)	0.72 (0.15),	1.09 (0.29)	1 (1,2)	
Stratification				1000			
Regression	6.0	100	0.70 (0.15)	0.70 (0.15),	1.11 (0.33)	1 (1,2)	
				1000			

Table B9-6. Common treatment and common outcome, cumulative estimation method, and scenario 3



IX. APPENDIX C

SITE	YEAR OF	GI BLEED WITH	HIN 6 MONTHS	TYPE OF NSAID DRUG		
	DRUG	No	Yes	Non-selective NSAID	COX-2 NSAID	
	INITIATION	N (%)	N (%)	N (%)	N (%)	
1	2008	330014	484	315716	14782	
		(99.85%)	(0.15%)	(95.53%)	(4.47%)	
	2009	542085	756	524890	17951	
		(99.86%)	(0.14%)	(96.69%)	(3.31%)	
	2010	427690	548	416326	11912	
		(99.87%)	(0.13%)	(97.22%)	(2.78%)	
	2011	366124	479	358455	8148	
		(99.87%)	(0.13%)	(97.78%)	(2.22%)	
2	2008	193535	392	183781	10146	
		(99.80%)	(0.20%)	(94.77%)	(5.23%)	
	2009	162160	340	156018	6482	
		(99.79%)	(0.21%)	(96.01%)	(3.99%)	
	2010	144572	300	139656	5216	
		(99.79%)	(0.21%)	(96.40%)	(3.60%)	
	2011	139742	286	135141	4887	
		(99.80%)	(0.20%)	(96.51%)	(3.49%)	
15	2008	107165	53	106998	220	
		(99.95%)	(0.05%)	(99.79%)	(0.21%)	
	2009	96063	47	95870	240	
		(99.95%)	(0.05%)	(99.75%)	(0.25%)	
	2010	88133	41	87939	235	
		(99.95%)	(0.05%)	(99.73%)	(0.27%)	
	2011	87914	42	87640	316	
		(99.95%)	(0.05%)	(99.64%)	(0.36%)	

Table C1. Incident GI bleed within six months and type of NSAID exposures by year and site

Table C2. Incident GI bleed outcome: results for Propensity Score matched samples (4:1) (4 Nonselective NSAIDs matched to 1 COX-2) ; Full cohort with matches not restricted to caliper of +0.05

Look	Time ¹	Nonselective NSAID		COX-2 NSAID		HR ^₄ Nonselective	Sequential analysis	Test statistic	Signal ⁷
		GI bleeds	Person years _{cum} ³	GI bleeds	Person years _{cum}	NSAID vs COX-2	test statistic⁵	boundary ⁶	
		cum ²		cum					
Lookwi	se PS ⁸								
1	2008	287	45849	63	11510	1.15	0.968	2.1040	No
2	2009	603	90831	130	22824	1.17	1.613	2.0323	No
3	2010	824	122314	174	30703	1.19	2.116	2.0514	Yes
4	2011	995	146961	224	36878	1.12	1.511	2.0508	
Cumula	ative PS ⁹								
1	2008	294	45864	63	11510	1.18	1.199	2.1040	No
2	2009	600	90865	130	22824	1.16	1.552	2.0323	No
3	2010	804	122337	174	30703	1.17	1.812	2.0514	No
4	2011	976	147016	224	36878	1.09	1.178	2.0508	No

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group)

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group)

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores

Table C3. Incident GI bleed outcome: results for Disease Risk Score matched samples (4:1) (4 Nonselective NSAIDs matched to 1 COX-2); Full cohort with matches not restricted to caliper of +0.05

Look	Time ¹	Nonsele	ctive NSAID	COX-2 NSAID		HR ⁴ Nonselective	Sequential analysis	Test statistic	Signal ⁷
		GI	Person	GI	Person	NSAID vs	test	boundary ⁶	
		bleeds	years _{cum} s	bleedsc	years _{cum}	COX-2	statistic⁵		
		cum ²		um					
Lookwi	se DRS ⁸								
1	2008	318	45765	63	11510	1.32	1.972	2.1040	No
2	2009	666	90704	130	22824	1.32	2.857	2.0323	Yes
3	2010	892	122154	174	30703	1.32	3.323	2.0514	
4	2011	1061	146843	224	36878	1.22	2.647	2.0508	
Cumula	tive DRS	9							
1	2008	311	45772	63	11510	1.29	1.820	2.1040	No
2	2009	651	90726	130	22824	1.31	2.759	2.0323	Yes
3	2010	848	122205	174	30703	1.27	2.821	2.0514	
4	2011	1017	146876	224	36878	1.18	2.194	2.0508	

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group)

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group)

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test Statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores



Look	Time ¹	Nonse NS	elective GAID	COX-2 NSAID		HR⁴ Nonselective NSAID vs	Sequential analysis test	Test statistic boundary ⁶	Signal ⁷
		GI bleeds _{cum²}	Person years _{cum} 3	GI bleedsc um	Person years _{cum}	COX-2	statistic⁵	,	
Lookwi	se PS ⁸	L	L						
1	2008	70	11451	63	11510	1.24	1.170	2.1040	No
2	2009	134	22683	130	22824	1.09	0.699	2.0323	No
3	2010	179	30563	174	30701	1.08	0.658	2.0514	No
4	2011	223	36712	224	36877	1.04	0.389	2.0508	No
Cumula	tive PS ⁹					•		•	
1	2008	66	11459	63	11510	1.20	1.007	2.1040	No
2	2009	134	22689	130	22824	1.07	0.505	2.0323	No
3	2010	178	30563	174	30701	1.06	0.495	2.0514	No
4	2011	230	36728	224	36877	1.04	0.387	2.0508	No

Table C4. Incident GI bleed outcome: results for Propensity matched samples (1:1) (1 Nonselective NSAIDs matched to 1 COX-2)

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group)

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group)

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores


Table C5. Incident GI bleed outcome: results for Disease Risk Score matched samples (1:1) (1Nonselective NSAIDs matched to 1 COX-2)

Look	Time ¹	Nonselective NSAID		COX-2 NSAID		HR ⁴ Nonselective	Sequential analysis	Test statistic	Signal ⁷
		GI bleeds _{cum²}	Person years _{cum} ³	GI bleeds ^{cum}	Person years _{cum}	NSAID vs COX-2	test statistic ⁵	boundary ⁶	
Lookwise DRS ⁸									
1	2008	82	11349	63	11403	1.51	2.325	2.1040	Yes
2	2009	163	22426	130	22602	1.34	2.399	2.0323	
3	2010	208	30184	174	30366	1.24	2.054	2.0514	
4	2011	254	36191	224	36388	1.18	1.744	2.0508	
Cumulative DRS ⁹									
1	2008	86	11341	63	11403	1.51	2.366	2.1040	Yes
2	2009	169	22437	130	22602	1.31	2.781	2.0323	
3	2010	212	30193	174	30366	1.27	2.612	2.0514	
4	2011	252	36208	224	36388	1.18	2.075	2.0508	

¹Timing of each look; Later looks include information from the preceding time intervals

²GI bleeds_{cum} is the total number of incident GI bleed events up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

³Person years_{cum} is the total accumulated exposure time up to and including the year of each look (within each selected drug group), only two sites included due to DRS data issues at third site

⁴HR is the hazard ratio for nonselective NSAID vs COX-2 drugs for all times up to and including each look

⁵Test Statistic is the drug comparison parameter estimate / standard error from the proportional hazards model

⁶Test statistic boundary: sequential analysis boundary estimate

⁷Signal indicates when the test statistic first exceeds the test statistic boundary

⁸Lookwise estimation used single year data when estimating scores

⁹Cumulative estimation used all years up to and including the current year when estimating scores